

Exotic charged current interactions in tritium beta decay

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Talk based on P.O.L., W. Rodejohann (MPIK Heidelberg): [arXiv:1603.08690](https://arxiv.org/abs/1603.08690)

Outline of the talk

- I. Direct neutrino mass experiments
- II. Physics of tritium beta decay
- III. Exotic CC interactions in tritium beta decay
- IV. Summary and conclusions

I. Direct neutrino mass experiments

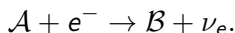
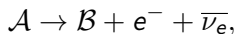
Neutrino mass bounds from direct neutrino mass experiments

- Bounds from **direct neutrino mass experiments**: Mainz and Troitsk experiment [hep-ex/0412056; 1108.5034]:
Precise study of the endpoint of the tritium beta spectrum.

$$\rightarrow m_\nu < 2 \text{ eV}.$$

Direct neutrino mass experiments are important to confirm/challenge cosmological observations and $m_{\beta\beta}$ bounds.

Generic method of direct neutrino mass experiments: Measurement of endpoint of β -spectrum or electron capture spectrum:



Direct neutrino mass experiments

Ideal isotopes: Q-value as small as possible $\rightarrow m_\nu \neq 0$ has largest effect on spectrum.

- **Tritium:** ${}^3\text{H} \rightarrow {}^3\text{He}^+ + e^- + \bar{\nu}_e$ ($Q = 18.6$ keV),
- **Holmium:** ${}^{163}\text{Ho}^+ + e^- \rightarrow {}^{163}\text{Dy} + \nu_e$ ($Q = 2.8$ keV)

Experiments: See talk by Loredana Gastaldo.

- **KATRIN** (see talk by Guido Drexlin): tritium beta spectrum,
- **Project 8:** tritium beta spectrum,
- **PTOLEMY** (see talk by Alfredo Cocco): tritium beta spectrum,
- **NuMECS, HOLMES, ECHo:** Holmium electron capture spectrum.

What can we learn from direct neutrino mass experiments?

- Study of the endpoint of the energy spectrum: Bounds on the absolute neutrino mass scale,
- search for eV-scale sterile neutrinos, ... → see talk by Guido Drexlin.

What else?

Example: The KATRIN tritium source has an activity of about 10^{11} decays per second

→ If experimental setup can be upgraded for measuring the **whole spectrum**: TRISTAN (see talks by Guido Drexlin and Thierry Lasserre):

→ **Ultra-high statistics and ultra-high precision measurement of the tritium beta spectrum.**

What can we learn from extensions of KATRIN-like experiments?

Ultra-high statistics and ultra-high precision measurement of the tritium beta spectrum.

This can even lead to bounds on (or discovery of) **new physics** provided that

the standard model physics involved in beta decay is sufficiently well understood.

For a review on this issue see Susanne Mertens *et al.* [1409.0920] and the talk by Thierry Lasserre.

For the research project presented in this talk: Assumed that sufficient understanding is given.

What can we learn from extensions of KATRIN-like experiments?

In our paper we studied three effects:

- **Difference relativistic / non-relativistic treatment of the spectrum,**
- **spectral distortion from new charged-current (CC) interactions**
- **for light active and keV sterile neutrinos**

II. Physics of tritium beta decay

Kinematics of β decay

$$\mathcal{A} \rightarrow \mathcal{B} + e^- + \bar{\nu}_e$$

$$|\bar{\nu}_e\rangle = \sum_{j=1}^{3+n_s} U_{ej} |\nu_j\rangle$$

Fully relativistic treatment of 3-body decay gives

$$\left(\frac{d\Gamma}{dE_e}\right)_{\bar{\nu}_j} = \frac{1}{64\pi^3 m_{\mathcal{A}}} \int_{E_j^-}^{E_j^+} dE_j |\mathcal{M}(\mathcal{A} \rightarrow \mathcal{B} + e^- + \bar{\nu}_j)|^2$$

- E_j^\pm min. and max. neutrino energy (function of particle masses and E_e).
- $|\mathcal{M}(\mathcal{A} \rightarrow \mathcal{B} + e^- + \bar{\nu}_j)|^2$ squared matrix element (unpolarized): function of particle masses and E_e and E_j .

Theoretical framework

- Lorentz invariance,
- only tree-level interactions,
- only effective four-fermion interactions,
- no assumption about the Lorentz structure \rightarrow all types of interactions allowed (scalar, vector, axial vector, ...)

Under these assumptions the amplitude \mathcal{M} has the form

$$\mathcal{M} = [\bar{u}_e \mathcal{O} v_j][\bar{u}_B \mathcal{O}' u_A].$$

If operators \mathcal{O} and \mathcal{O}' independent of particle momenta, $|\mathcal{M}|^2$ contains only terms of the form

$$(p \cdot p') \quad \text{or} \quad (p \cdot p')(p'' \cdot p''').$$

Theoretical framework

$$\mathcal{M} \sim (p \cdot p') \quad \text{or} \quad (p \cdot p')(p'' \cdot p''')$$

→ Energy-momentum conservation: $p_A = p_B + p_e + p_j$

⇒ $p \cdot p'$ depends only on E_e (electron energy) and E_j (neutrino energy).

$$|\mathcal{M}(A \rightarrow B + e^- + \bar{\nu}_j)|^2 = A + B_1 E_e + B_2 E_j + C E_e E_j + D_1 E_e^2 + D_2 E_j^2,$$

⇒ **The energy spectrum in our framework can be parameterized by six parameters!**

In a given model A , B_1 , B_2 , C , D_1 and D_2 depend on the particle masses and coupling constants only!

Relativistic electron energy spectrum

$$\begin{aligned}\left(\frac{d\Gamma}{dE_e}\right)_{\bar{\nu}_j} &= \frac{1}{64\pi^3 m_{\mathcal{A}}} \int_{E_j^-}^{E_j^+} dE_j |\mathcal{M}(\mathcal{A} \rightarrow \mathcal{B} + e^- + \bar{\nu}_j)|^2 \\ &= \frac{1}{64\pi^3 m_{\mathcal{A}}} \times \\ &\quad \left\{ (A + B_1 E_e + D_1 E_e^2)(E_{j+} - E_{j-}) + \right. \\ &\quad \left. \frac{1}{2}(B_2 + C E_e)(E_{j+}^2 - E_{j-}^2) + \right. \\ &\quad \left. \frac{1}{3} D_2 (E_{j+}^3 - E_{j-}^3) \right\}.\end{aligned}$$

Effect of relativistic/non-relativistic spectrum

- Effect on spectral endpoint position:

$$(E_e^{\max})_{\text{NR}} = m_A - m_B - m_j,$$
$$(E_e^{\max})_{\text{R}} = \frac{m_A^2 + m_e^2 - (m_B + m_j)^2}{2m_A}.$$

Difference for tritium decay: $\approx 3.4 \text{ eV}$.

- **Whole spectrum: Difference is of the order of $\approx 10^{-4} \div 10^{-3}$.**

In the following: Show “textbook example”: Standard model expression relativistic/non-relativistic.

Example: Standard model: relativistic/non-relativistic

$$\mathcal{L} = -\frac{G_F}{\sqrt{2}} V_{ud} \left(\bar{e} \gamma^\mu (\mathbb{1} - \gamma^5) \nu_e \right) \left(\bar{B} \gamma_\mu (g_V \mathbb{1} - g_A \gamma^5) \mathcal{A} \right) + \text{H.c.}$$

\Rightarrow

$$A = \frac{\gamma}{2} m_{\mathcal{A}} m_{\mathcal{B}} (g_V^2 - g_A^2) (m_{\mathcal{A}}^2 - m_{\mathcal{B}}^2 + m_e^2 + m_j^2),$$

$$B_1 = \frac{\gamma}{2} m_{\mathcal{A}} \left\{ (g_V - g_A)^2 (m_{\mathcal{A}}^2 - m_{\mathcal{B}}^2 + m_e^2 - m_j^2) - 2m_{\mathcal{A}} m_{\mathcal{B}} (g_V^2 - g_A^2) \right\},$$

$$B_2 = \frac{\gamma}{2} m_{\mathcal{A}} \left\{ (g_V + g_A)^2 (m_{\mathcal{A}}^2 - m_{\mathcal{B}}^2 - m_e^2 + m_j^2) - 2m_{\mathcal{A}} m_{\mathcal{B}} (g_V^2 - g_A^2) \right\},$$

$$C = 0,$$

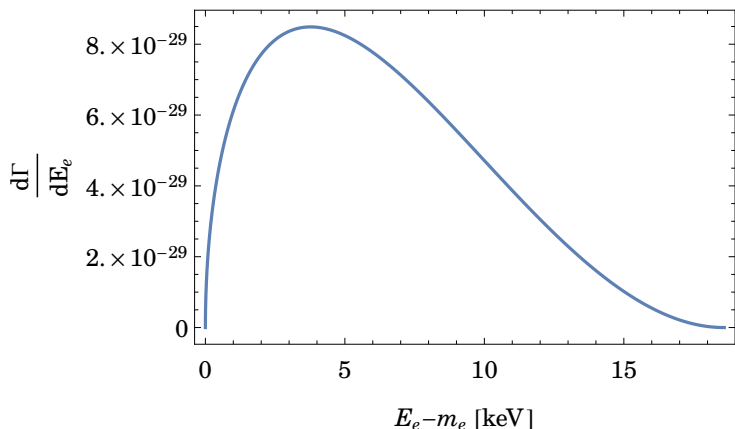
$$D_1 = -\gamma m_{\mathcal{A}}^2 (g_V - g_A)^2,$$

$$D_2 = -\gamma m_{\mathcal{A}}^2 (g_V + g_A)^2,$$

$$\gamma \equiv 16 G_F^2 |V_{ud}|^2 |U_{ej}|^2.$$

Example: Standard model: relativistic/non-relativistic

Standard model β -spectrum for tritium decay:

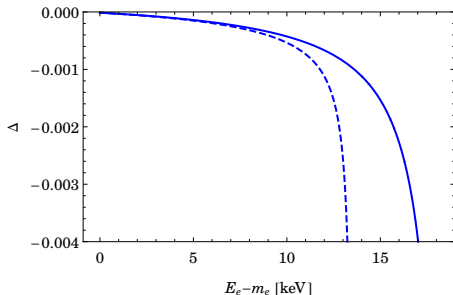


Example: Standard model: relativistic/non-relativistic

Non-relativistic approximation is the leading term in the expansion $\frac{\text{energy scale}}{m_A}$

$$\rightarrow \left(\frac{d\Gamma}{dE_e} \right)_{\text{NR}, m_j=0} = \frac{2 G_F^2 |V_{ud}|^2}{\pi^3} |\vec{p}_e| E_e (m_A - m_B - E_e)^2.$$

Deviation relativistic/non-relativistic expression: $\Delta \equiv \frac{(d\Gamma/dE_e) - (d\Gamma/dE_e)_{\text{NR}}}{(d\Gamma/dE_e)_{\text{NR}}}$.



Solid: $m_j = 0$; dashed: $m_j = 5 \text{ keV}$.

Deviation $\sim 10^{-4} \div 10^{-3}$

III. Exotic CC interactions in tritium beta decay

Lagrangian

Effective operator approach: All possible Lorentz-invariant interactions. Use notation of Cirigliano *et al.* [1303.6953]. $L = \mathbb{1} - \gamma^5$. Add RH ν s.

$$\mathcal{L}_{\text{CC}} = -\frac{G_F V_{ud}}{\sqrt{2}} \left\{ (1 + \delta_\beta)(\bar{e}L_\mu\nu_e)(\bar{u}L^\mu d) + \sum_j \overset{(\sim)}{\epsilon}_j (\bar{e}O_j\nu_e)(\bar{u}O'_j d) \right\} + \text{H.c.}$$

$\overset{(\sim)}{\epsilon}_j$	O_j	O'_j
ϵ_L	$\gamma_\mu(\mathbb{1} - \gamma_5)$	$\gamma^\mu(\mathbb{1} - \gamma_5)$
$\tilde{\epsilon}_L$	$\gamma_\mu(\mathbb{1} + \gamma_5)$	$\gamma^\mu(\mathbb{1} - \gamma_5)$
ϵ_R	$\gamma_\mu(\mathbb{1} - \gamma_5)$	$\gamma^\mu(\mathbb{1} + \gamma_5)$
$\tilde{\epsilon}_R$	$\gamma_\mu(\mathbb{1} + \gamma_5)$	$\gamma^\mu(\mathbb{1} + \gamma_5)$
ϵ_S	$\mathbb{1} - \gamma_5$	$\mathbb{1}$
$\tilde{\epsilon}_S$	$\mathbb{1} + \gamma_5$	$\mathbb{1}$
$-\epsilon_P$	$\mathbb{1} - \gamma_5$	γ^5
$-\tilde{\epsilon}_P$	$\mathbb{1} + \gamma_5$	γ^5
ϵ_T	$\sigma_{\mu\nu}(\mathbb{1} - \gamma_5)$	$\sigma^{\mu\nu}(\mathbb{1} - \gamma_5)$
$\tilde{\epsilon}_T$	$\sigma_{\mu\nu}(\mathbb{1} + \gamma_5)$	$\sigma^{\mu\nu}(\mathbb{1} + \gamma_5)$

Two basic types of couplings: ϵ : left-handed ν s, $\tilde{\epsilon}$: right-handed ν s.

Numerical analysis

Bounds for the coefficients ϵ and $\tilde{\epsilon}$ from Cirigliano *et al.* [1303.6953].

parameter	best 90% CL upper bound		used for our estimation
	$ \text{Re } \epsilon $	$ \text{Im } \epsilon $	ϵ
ϵ_L	5×10^{-4}	5×10^{-3}	5.0×10^{-3}
$\tilde{\epsilon}_L$	6×10^{-2}	—	8.5×10^{-2}
ϵ_R	5×10^{-4}	5×10^{-4}	7.1×10^{-4}
$\tilde{\epsilon}_R$	5×10^{-3}	5×10^{-3}	7.1×10^{-3}
ϵ_S	8×10^{-3}	1×10^{-2}	1.3×10^{-2}
$\tilde{\epsilon}_S$	1.3×10^{-2}	1.3×10^{-2}	1.8×10^{-2}
ϵ_P	4×10^{-4}	2×10^{-4}	4.5×10^{-4}
$\tilde{\epsilon}_P$	2×10^{-4}	2×10^{-4}	2.8×10^{-4}
ϵ_T	1×10^{-3}	1×10^{-3}	1.4×10^{-3}
$\tilde{\epsilon}_T$	3×10^{-3}	3×10^{-3}	4.2×10^{-3}

Procedure for numerical analysis

- Fixed neutrino masses $m_j = 0.5 \text{ eV}$ (light active neutrinos) or
- $m_j = 5 \text{ keV}$ (heavy sterile right-handed neutrino), see talk by Alex Merle,
- one ϵ or $\tilde{\epsilon}$ set to 1, the others set to 0,
- relevant mixing matrix element set to 1.

→ Computed the values for the six coefficients A, \dots, D_2 .

→ Tables in paper.

Paper gives prescription how to scale the tabulated values for other values of ϵ and other mixing matrix elements.

⇒ **Can directly obtain the beta spectrum for any new CC interaction.**

Signal to be expected in a high-precision experiment

Mixing active/sterile (left/right) is of the order of

$$\frac{m_{\text{light}}}{m_{\text{heavy}}} \lesssim \frac{\text{eV}}{\text{keV}} \sim 10^{-3}.$$

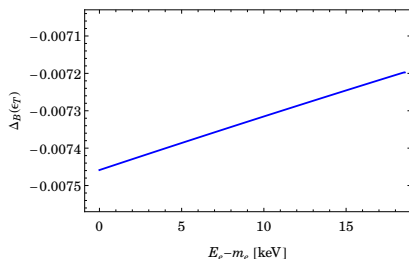
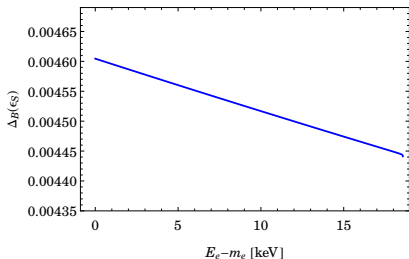
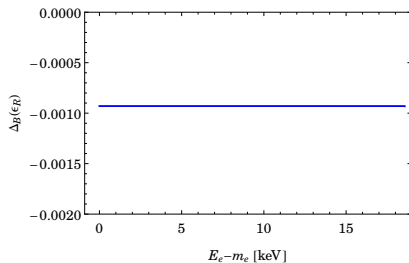
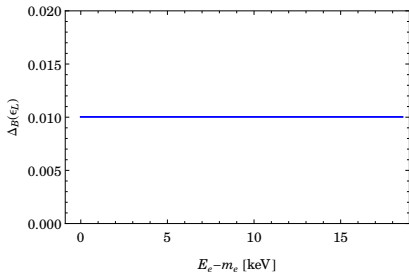
⇒ “heavy neutrinos/ ϵ ” and “light neutrinos/ $\tilde{\epsilon}$ ”: **strongly suppressed by mixing matrix** → **no observable effect.**

- ϵ : studied light neutrinos ($m_j = 0.5 \text{ eV}$),
- $\tilde{\epsilon}$: heavy neutrinos ($m_j = 5 \text{ keV}$).
- Used upper bounds for ϵ and $\tilde{\epsilon}$ from literature.

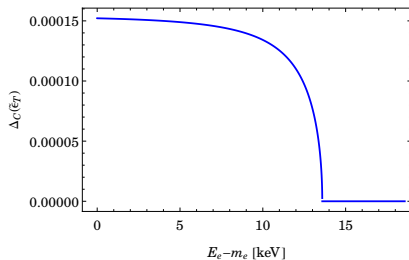
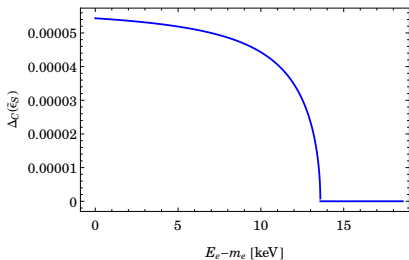
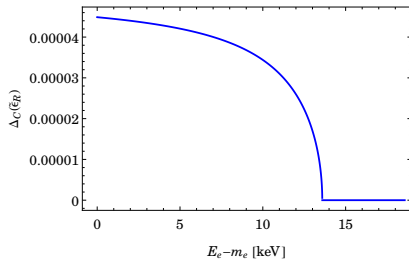
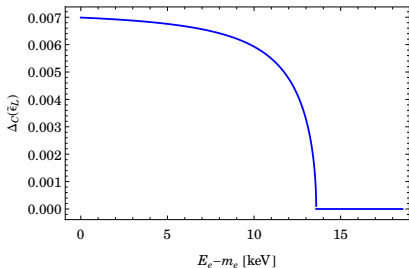
→ Plots of:

$$\Delta(\tilde{\epsilon}_j) \equiv \frac{\text{test spectrum (NP)} - \text{reference spectrum (no NP)}}{\text{reference spectrum (no NP)}}.$$

New physics effects for light neutrinos with $m_j = 0.5 \text{ eV}$



New physics effects for heavy neutrinos with $m_j = 5 \text{ keV}$



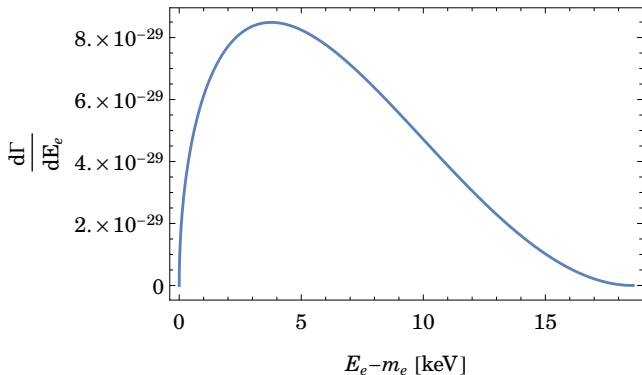
Summary

- Upgraded KATRIN (or KATRIN-like) experiment may have access to the full energy spectrum of tritium decay. → Ultra-high statistics and ultra-high precision!
- Fully relativistic calculation of the β spectrum. Generic spectrum depends on six process-dependent parameters.
- Departure from usual non-relativistic approximation: $\approx 10^{-4} \div 10^{-3}$.
- New physics in β decay: Studied all possible new CC interactions in effective operator framework.
- Both light (sub-eV) and heavy (keV) neutrinos considered: Effect on endpoints negligible, full spectrum can show sizable distortions at the permille level.

Conclusions

- Accessibility of the new-physics effects by a future KATRIN-like experiment: Example: keV scale right-handed neutrinos: Sensitivity estimate (Mertens *et al.* [1409.0920]): $\sim 10^{-7}$.
- \rightarrow modified KATRIN-like setup sensitive to
 - $\epsilon_L, \epsilon_R, \epsilon_S, \epsilon_T$ in case of light left-handed (even almost massless) neutrinos.
Different new-physics scenarios can be distinguished by the shape of the spectral distortion;
 - $\tilde{\epsilon}_L, \tilde{\epsilon}_R, \tilde{\epsilon}_S, \tilde{\epsilon}_T$ in case of keV-scale right-handed neutrinos.
New physics effects are not easily distinguishable (shapes are quite similar).
- **If systematic effects in the experiment and all Standard Model contributions are under control, an extended KATRIN-like setup may significantly improve the bounds on new CC interactions in β decay.**

Thank you for your attention!

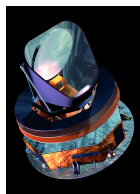


Backup slides

Current bounds on neutrino masses

- Bounds from **cosmology**: Bounds on the sum of the three active neutrino masses:

$$\begin{aligned}\sum m_\nu &< 0.72 \text{ eV} && \text{Planck TT+lowP,} \\ \sum m_\nu &< 0.21 \text{ eV} && \text{Planck TT+lowP+BAO,} \\ \sum m_\nu &< 0.49 \text{ eV} && \text{Planck TT, TE, EE+lowP,} \\ \sum m_\nu &< 0.17 \text{ eV} && \text{Planck TT, TE, EE+lowP+BAO.}\end{aligned}$$



(Planck Collaboration [1502.01589]).

(Copyright: ESA. Illustration by Medialab.)

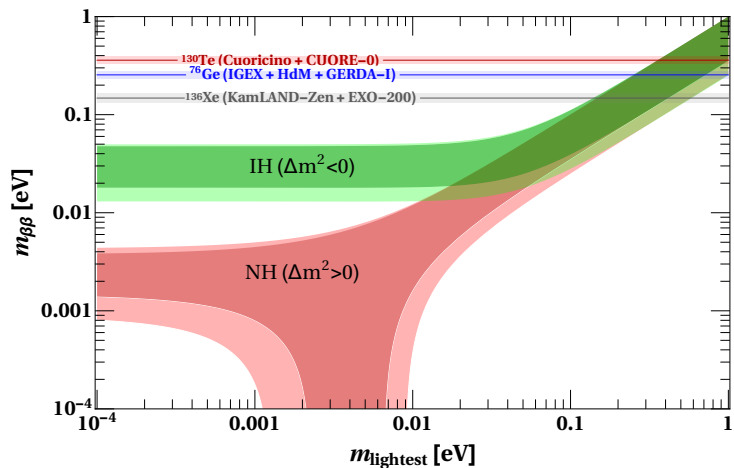
Dependent on which data taken into account. In any case **bound stronger than current direct neutrino mass bounds**.

- Bounds from **$(\beta\beta)_{0\nu}$ -searches**: Bounds on

$$m_{\beta\beta} = \left| \sum_{k=1}^3 U_{ek}^2 m_k \right| \rightarrow \text{bounds on absolute mass scale}$$

Current bounds on neutrino masses

Dell'Oro *et al.* [1601.07512]



$$m_\nu \lesssim \mathcal{O}(1 \text{ eV})$$

Minimal and maximal neutrino energy

$$E_{j\pm} = \frac{-(m_{\mathcal{A}} - E_e)(E_e m_{\mathcal{A}} - \alpha) \pm |\vec{p}_e| \sqrt{(E_e m_{\mathcal{A}} - \alpha + m_j^2)^2 - m_{\mathcal{B}}^2 m_j^2}}{m_{\mathcal{A}}^2 - 2m_{\mathcal{A}} E_e + m_e^2},$$

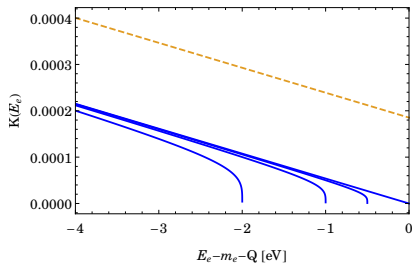
$$\alpha = \frac{1}{2} (m_{\mathcal{A}}^2 - m_{\mathcal{B}}^2 + m_e^2 + m_j^2).$$

Kurie plots

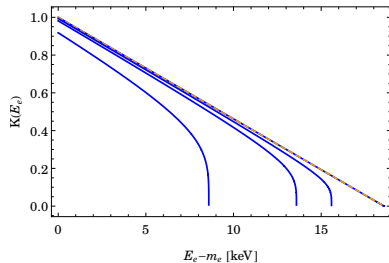
$$K(E_e) \equiv \frac{1}{m_A - m_B} \sqrt{\frac{d\Gamma/dE_e}{G_0(E_e)}},$$

where

$$G_0(E_e) \equiv \frac{2G_F^2 |V_{ud}|^2}{\pi^3} |\vec{p}_e| E_e F(Z, E_e).$$



$m_j = 2.0, 1.0, 0.5$ and 0 eV,



$10, 5, 3$ and 0 keV.

Momentum-dependent operators \mathcal{O} , \mathcal{O}'

In our study this case appears only for the *weak magnetism* correction:

$$\langle p(p_p) | \bar{u} \gamma_\mu d | n(p_n) \rangle = \bar{u}_p(p_p) \left[g_V(q^2) \gamma_\mu - i \frac{g_{WM}(q^2)}{2M_N} \sigma_{\mu\nu} q^\nu \right] u_n(p_n) + \mathcal{O}((q/M_N)^2)$$

$$q = p_A - p_B$$

Gives contribution to $|\mathcal{M}|^2$ of the form

$$\frac{(p \cdot q)(p' \cdot q)(p'' \cdot p''')}{M_N^2} \quad \text{or} \quad \frac{(p \cdot p')(p'' \cdot p''')(q \cdot q)}{M_N^2}.$$

For tritium decay suppressed by

$$\frac{q^2}{M_A^2} \lesssim 10^{-10}.$$

Corrections from Standard Model physics

See Susanne Mertens *et al.* [1409.0920] and the talk by Thierry Lasserre:

- **Excited final states:** the effect on the spectrum is very large—larger than 10 % close to the endpoint. Far from the endpoint $\sim 1\%$.
- Coulomb interaction between the outgoing electron, the daughter nucleus (\rightarrow **Fermi function** $F(Z, E_e)$) and the left behind orbital electron of the former ${}^3\text{H}_2$ -molecule.
- The **nuclear recoil: automatically taken into account** by using the exact relativistic expression for $d\Gamma/dE_e$.
- The **daughter nucleus** ${}^3\text{He}^{2+}$ is **not pointlike** \rightarrow modifies the Coulomb field acting on the emitted electron.
- **Radiative corrections:** The dominant radiative corrections will be **QED-corrections**. \rightarrow Of the order of $\sim 1\%$.
- **Hadronic matrix elements.**

Moreover, source is a gas at finite temperature (30K).

Corrections from Standard Model physics

Hadronic matrix elements: See Cirigliano *et al.* [1303.6953].

$$\langle p(p_p) | \bar{u} \gamma_\mu d | n(p_n) \rangle = \bar{u}_p(p_p) \left[g_V(q^2) \gamma_\mu - i \frac{g_{WM}(q^2)}{2M_N} \sigma_{\mu\nu} q^\nu \right] u_n(p_n) + \mathcal{O}((q/M_N)^2),$$

$$\langle p(p_p) | \bar{u} \gamma_\mu \gamma_5 d | n(p_n) \rangle = g_A(q^2) \bar{u}_p(p_p) \gamma_\mu \gamma_5 u_n(p_n) + \mathcal{O}((q/M_N)^2),$$

$$\langle p(p_p) | \bar{u} d | n(p_n) \rangle = g_S(q^2) \bar{u}_p(p_p) u_n(p_n),$$

$$\langle p(p_p) | \bar{u} \gamma_5 d | n(p_n) \rangle = g_P(q^2) \bar{u}_p(p_p) \gamma_5 u_n(p_n) = \mathcal{O}(q/M_N),$$

$$\langle p(p_p) | \bar{u} \sigma_{\mu\nu} d | n(p_n) \rangle = g_T(q^2) \bar{u}_p(p_p) \sigma_{\mu\nu} u_n(p_n) + \mathcal{O}(q/M_N).$$

Written here for proton and neutron. The same structure for tritium/ ^3He .

Values for form factors from measurements or lattice.

Neutrino mass states

$$\begin{pmatrix} U & S \\ T & V \end{pmatrix}^\dagger M_\nu \begin{pmatrix} U & S \\ T & V \end{pmatrix}^* = \text{diag}(m_1, m_2, m_3, M_1, \dots, M_s)$$

$$\nu_L = U \nu'_L + S N'_R{}^c,$$

$$\nu_R = T^* \nu'_L{}^c + V^* N'_R.$$

Choose (for numerical estimates) neutrino mass spectrum:

light neutrinos with $m_j = 0.5 \text{ eV}$ and heavy neutrinos with $m_j = 5 \text{ keV}$

→ see talk by Alex Merle.