

# Test of Non-Standard Interactions at Super-K

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Now2010, Sep. 6th, 2010  
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# Outline

- Introduction & Physics motivation
- Expected “NSI” phenomena at SK
- Data sets
- Analysis results
- Conclusions

# What is NSI ?

- Note: there are many non-standard interaction “NSI” in markets.

- In this analysis, NSI is defined as either

**FCNC**

$$\sigma(\nu_\alpha + f \rightarrow \nu_\beta + f) \neq 0 \quad \epsilon_{\alpha\beta}$$

and

**Non-universality(NU).**

$$\sigma(\nu_\alpha + f) \neq \sigma(\nu_\beta + f) \quad \epsilon_{\alpha\alpha}, \epsilon_{\beta\beta}$$

## NSI driven transition probability

$$H^{NSI} = \sqrt{2}G_F N_f(\vec{r}) \begin{pmatrix} \epsilon_{\mu\mu} & \epsilon_{\mu\tau} \\ \epsilon_{\mu\tau} & \epsilon_{\tau\tau} \end{pmatrix}$$



$$\epsilon \equiv \epsilon_{\mu\tau}$$

$$\epsilon' \equiv |\epsilon_{\mu\mu} - \epsilon_{\tau\tau}|$$

$$P_{\nu_\mu \rightarrow \nu_\mu} = 1 - \frac{4\epsilon^2}{4\epsilon^2 + \epsilon'^2} \sin^2(\sqrt{2}G_F \langle N_f \rangle L \sqrt{\epsilon'^2/4 + \epsilon^2})$$

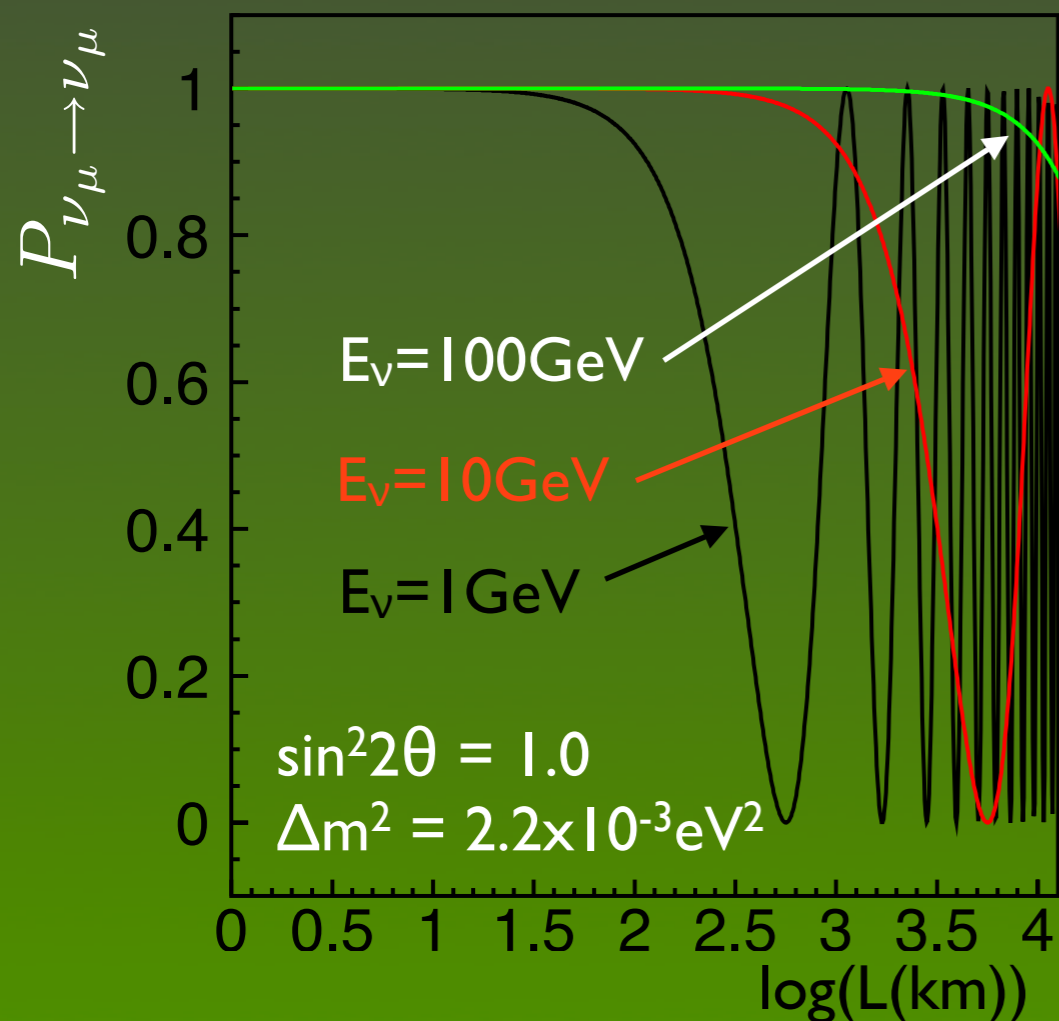
Probability changes as depending only on the number density “ $N_f$ ” and the flight length “ $L$ ”.



# Transition Probabilities

## Standard Oscillation

$$P_{\nu_\mu \rightarrow \nu_\mu} = 1 - \sin^2 2\theta \sin^2 \left( \frac{1.27 \Delta m^2 L}{E_\nu} \right)$$

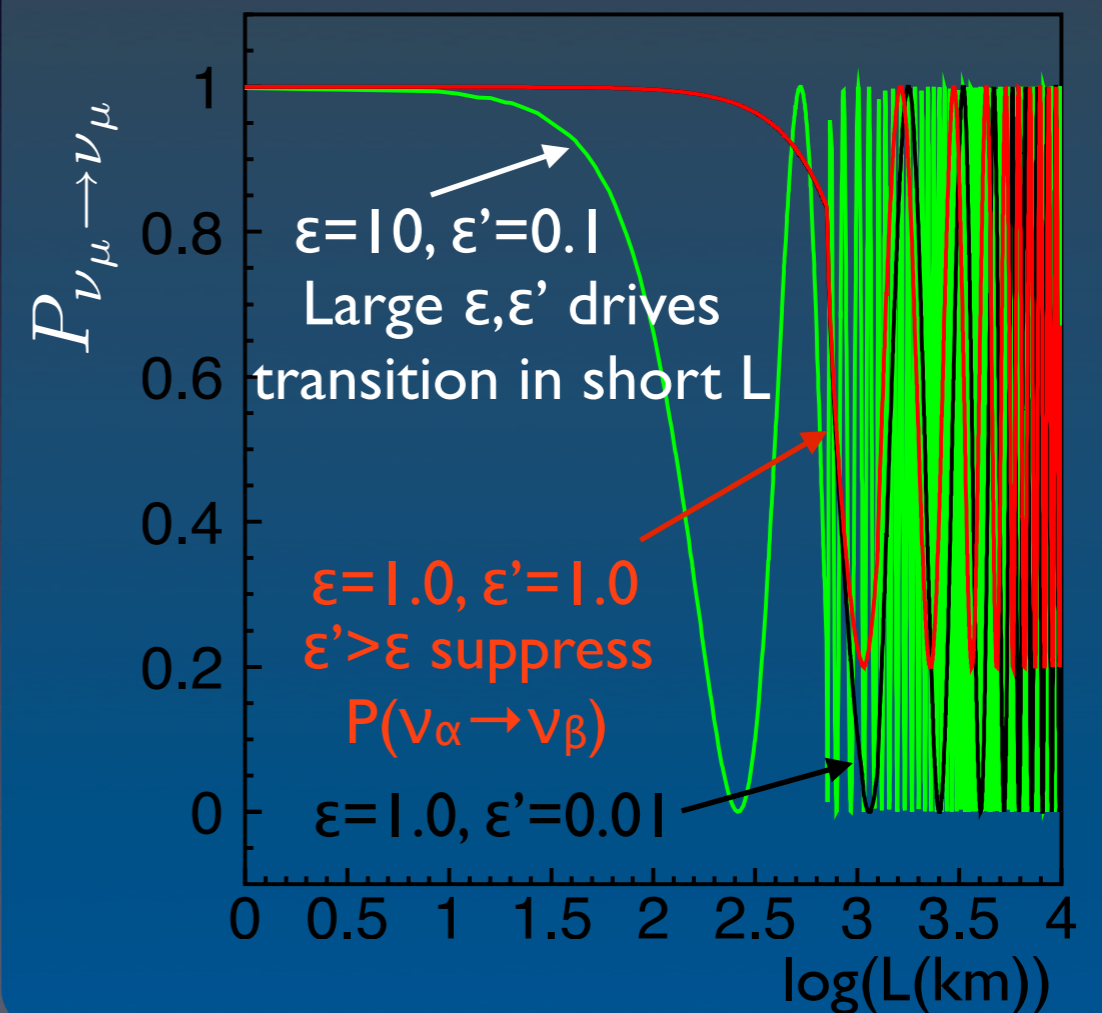


## NSI

$$P_{\nu_\mu \rightarrow \nu_\mu} = 1 - f(\varepsilon, \varepsilon') \sin^2(\sqrt{2} G_F \langle N_f \rangle L \varepsilon f(\varepsilon, \varepsilon'))$$

$$f(\varepsilon, \varepsilon') \equiv \frac{4\varepsilon^2}{4\varepsilon^2 + \varepsilon'^2}$$

$\varepsilon = \text{FCNC}$   
 $\varepsilon' = \text{NU}$



Sizable transition can occur in NSI even in high energy.

# $\nu$ NSI hunting ?

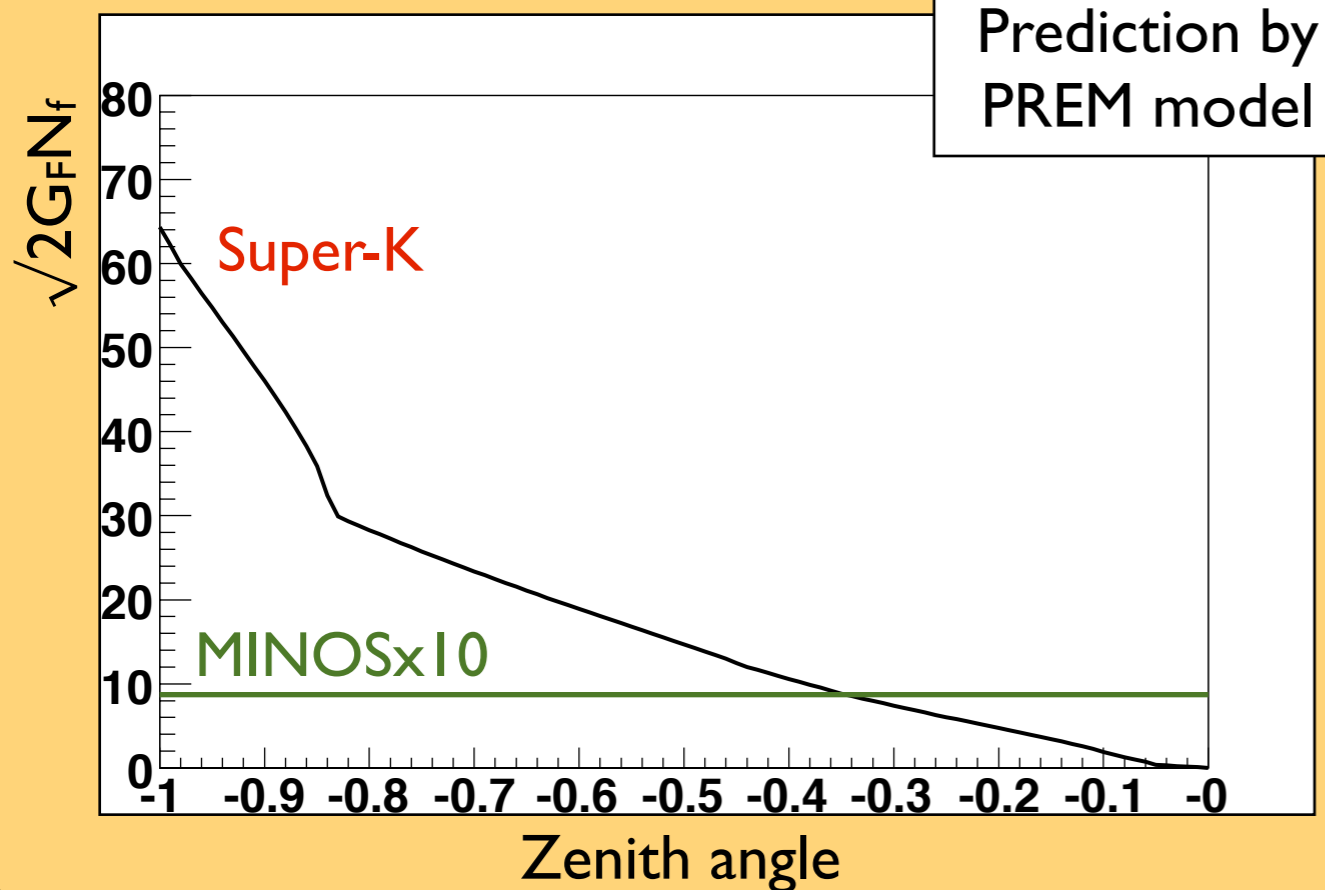
- Precise measurement of  $\nu$ -int. cross section  
CHARM, NuTeV, etc...
- Atmospheric neutrino  
Super-Kamiokande, MACRO
- Solar neutrino (matter  $\rightarrow$  vacuum transition)  
Borexino
- Accelerator neutrino  
 $\nu$  factory ?

NOTE: MACRO data is phenomenologically analyzed

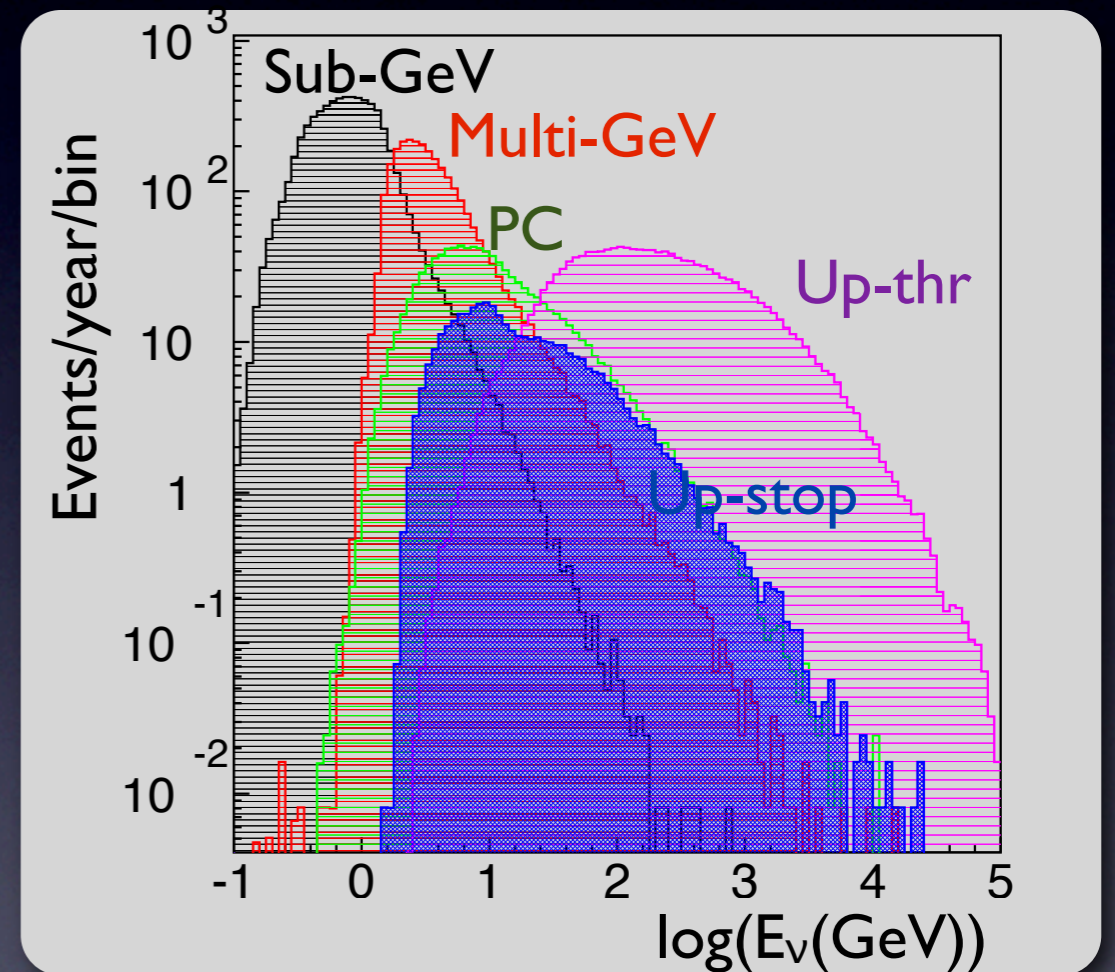


# Advantage of Super-K

*Fermion number density  
sensitive to FCNC & NU*



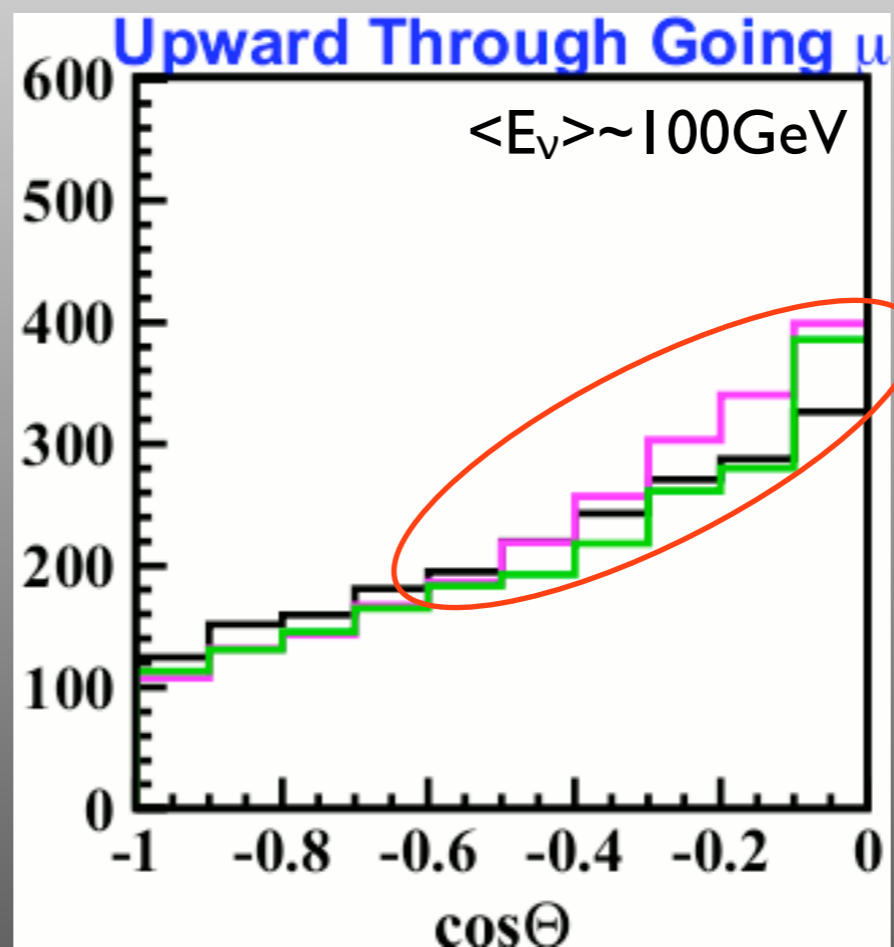
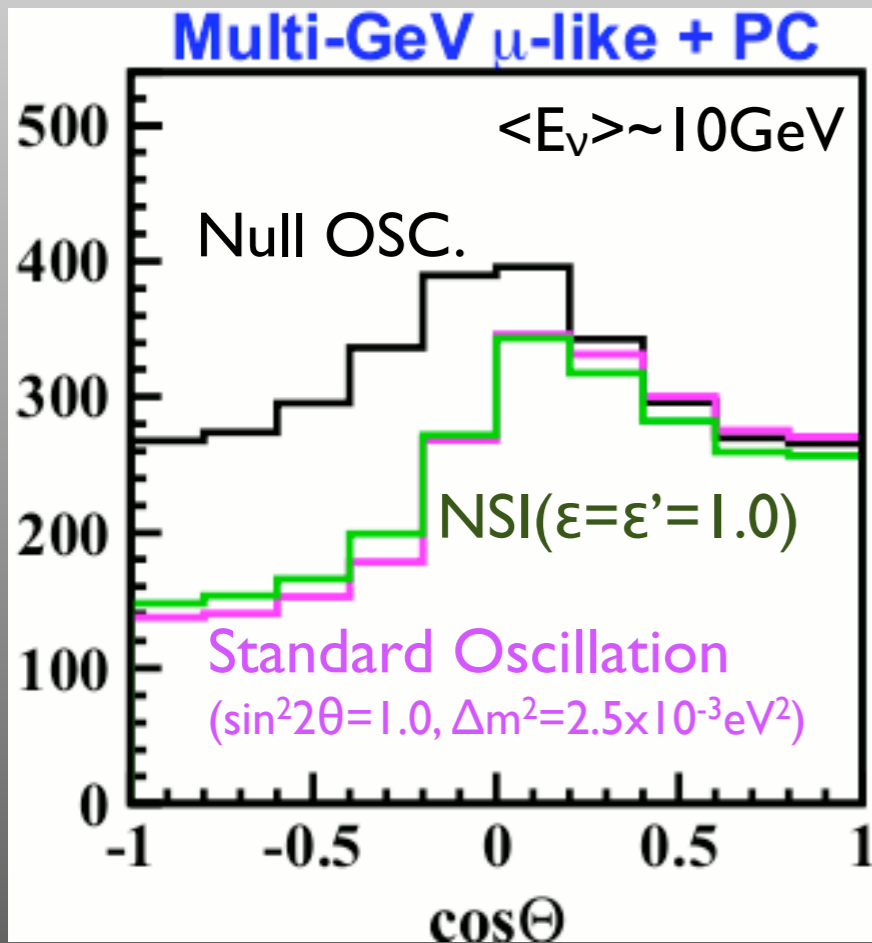
*Surveying wide range energy  
100MeV - 100TeV*



*Large number of events  
2,900 events/year @SK*

# Pure NSI $\Rightarrow$ Hybrid NSI

SK-I & SK-II



No significant inconsistency is in fully or partially contained event, while clear difference in Upward going  $\mu$ .

$\rightarrow$  Pure NSI scenario is ruled out.



*Hybrid NSI Model*

$$H_{\alpha\beta} = \frac{1}{2E} U_{\alpha j} \begin{pmatrix} 0 & 0 & 0 \\ 0 & \Delta m_{21}^2 & 0 \\ 0 & 0 & \Delta m_{31}^2 \end{pmatrix} (U^\dagger)_{k\beta} + V_{\text{MSW}} + \sqrt{2} G_F N_f(\vec{r}) \begin{pmatrix} \epsilon_{ee} & \epsilon_{e\mu}^* & \epsilon_{e\tau}^* \\ \epsilon_{e\mu} & \epsilon_{\mu\mu} & \epsilon_{\mu\tau}^* \\ \epsilon_{e\tau} & \epsilon_{\mu\tau} & \epsilon_{\tau\tau} \end{pmatrix}$$

Standard Oscillation NSI

*This talk presents the analyses based on the Hybrid model.*



# Analysis procedures

- Data&MC sets
  - FC, PC, and UP $\mu$  SK-I & II atm- $\nu$  data.
  - 2,280 livedays = 6.25years
  - MC statistics is 500years.
- Reconstruction tools and MC have been updated since the past oscillation analysis with SK-I and II.
- Agreement between data and MC is derived by checking “zenith angle” and “momentum” bins.
- Systematic errors related to neutrino flux, interaction, detector responses are taken into account (totally 90 terms).



# 2-Flavor Hybrid( $\mu\tau$ sector)

## 2-Flavor Hybrid model

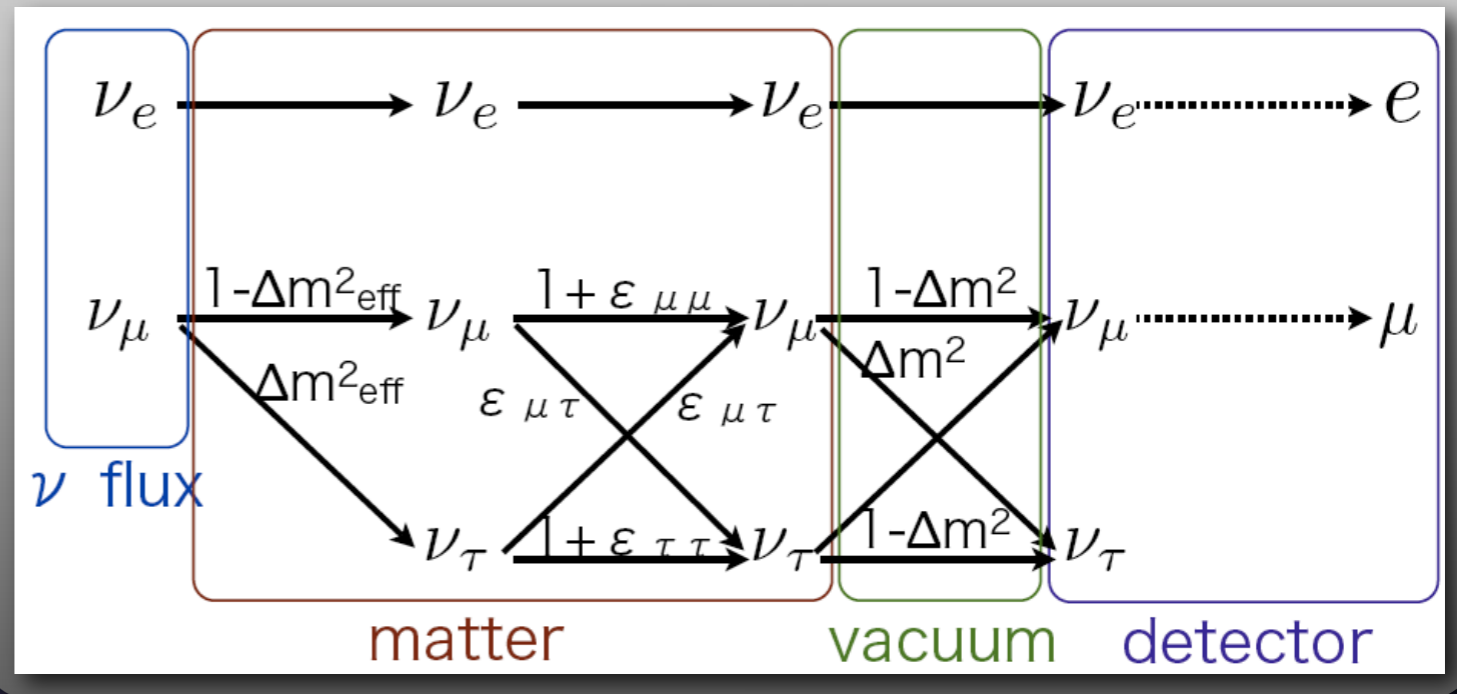
= 2-flavor OSC.( $2\leftrightarrow 3$ ) + 2-flavor NSI( $\mu\tau$ )

### NSI Hamiltonian

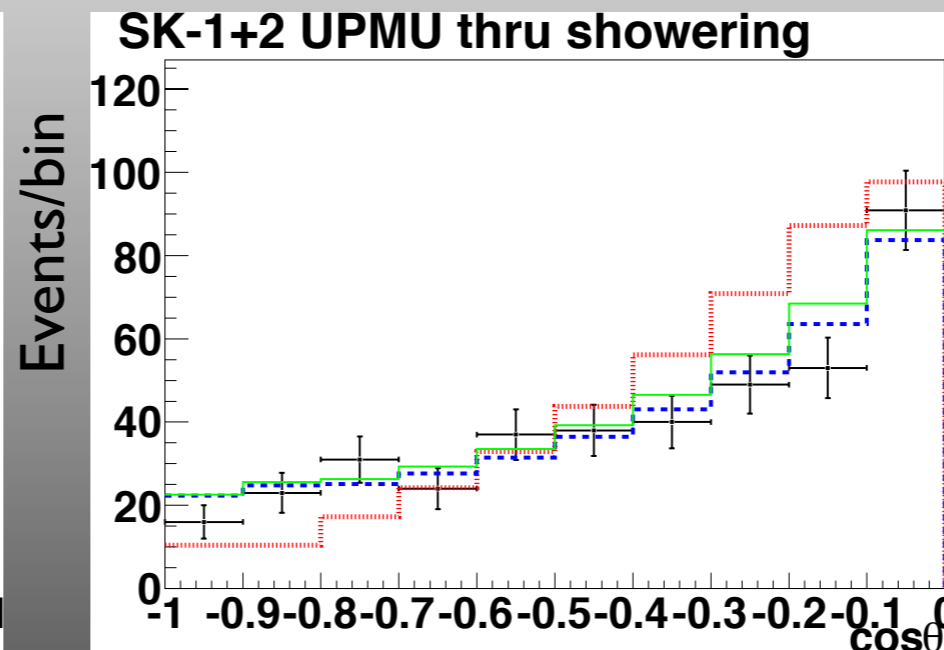
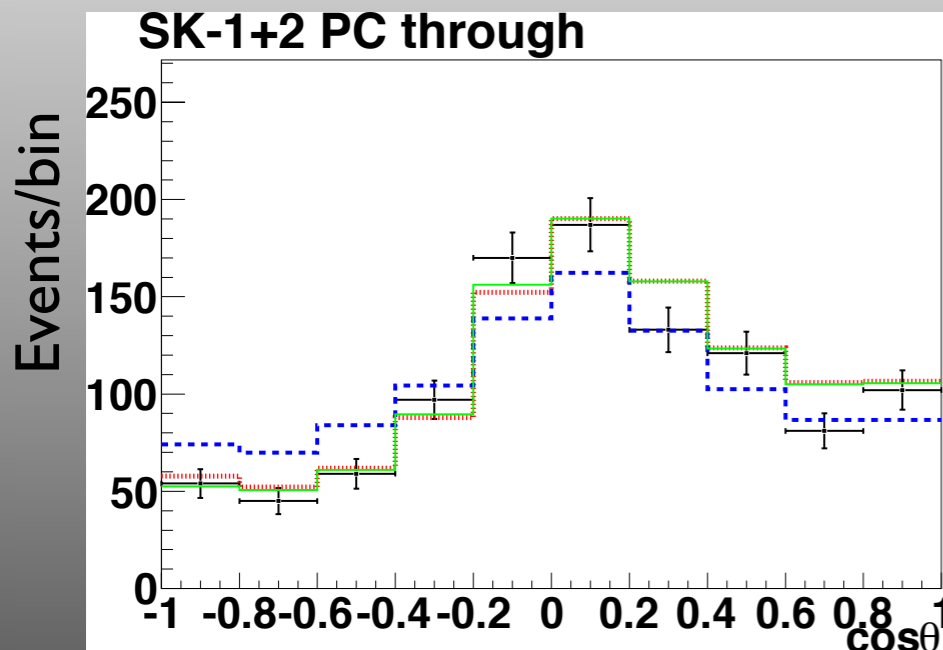
$$H_{\alpha\beta}^{NSI} = \sqrt{2}G_F N_f(\vec{r}) \begin{pmatrix} \epsilon_{ee} & \epsilon_{e\mu}^* & \epsilon_{e\tau}^* \\ \epsilon_{e\mu} & \epsilon_{\mu\mu} & \epsilon_{\mu\tau}^* \\ \epsilon_{e\tau} & \epsilon_{\mu\tau} & \epsilon_{\tau\tau} \end{pmatrix}$$

Focusing only on  $\mu\tau$  sector

Flavor transition from source to detector



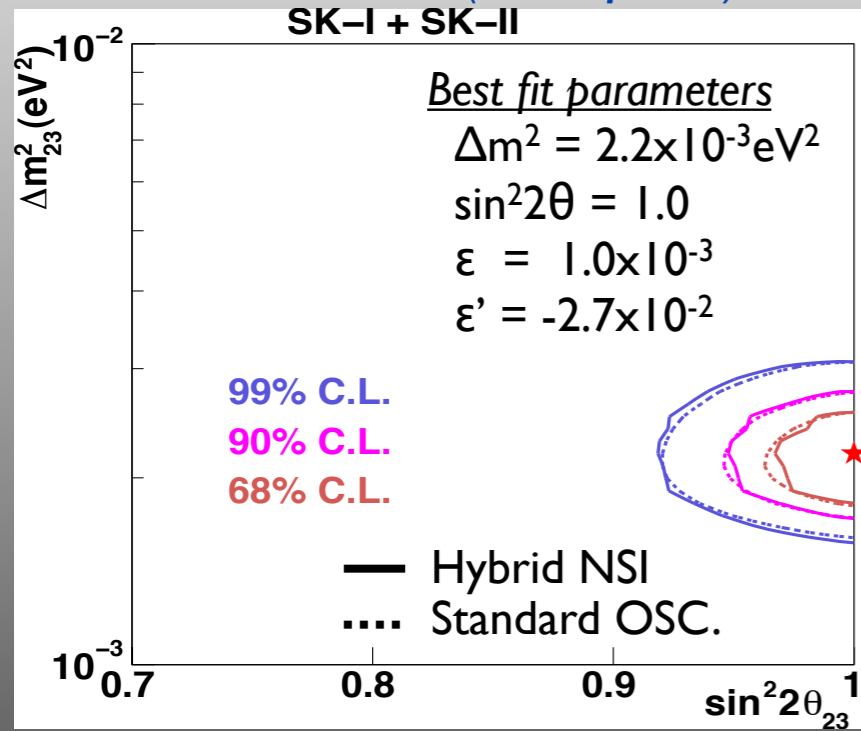
Zenith angle distributions with typical parameters



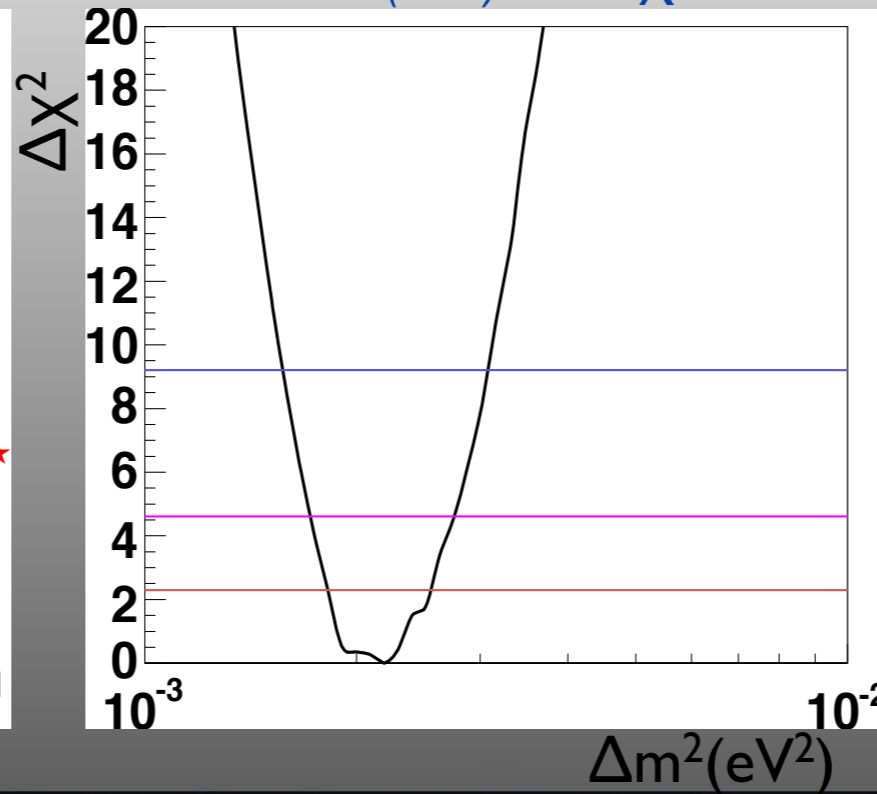
$\epsilon = \text{FCNC}$   
 $\epsilon' = \text{NU}$   
 $(\epsilon, \epsilon') =$   
 Green:  $(1.0 \times 10^{-3}, -2.4 \times 10^{-2})$   
 Blue:  $(1.0 \times 10^{-3}, -0.38)$   
 Red:  $(3.2 \times 10^{-3}, -2.4 \times 10^{-2})$   
 Note: All lines after  $\chi^2$  fitting with systematics.

# 2-Flavor Hybrid( $\mu\tau$ sector)

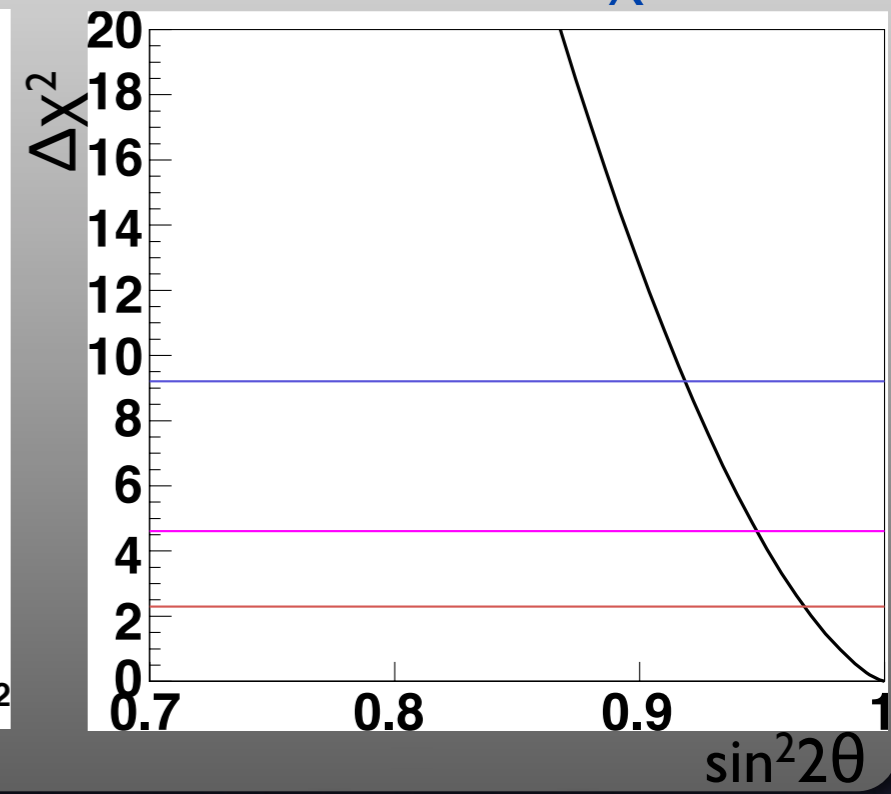
2D contour(OSC pars.)



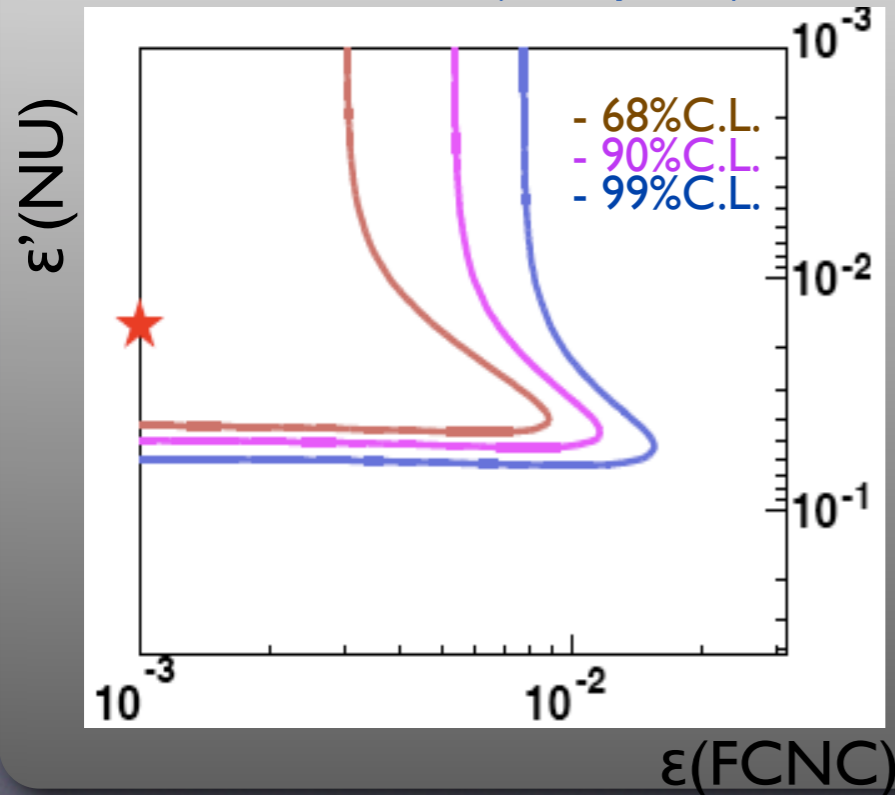
$\Delta m^2(\text{eV}^2)$  vs.  $\Delta\chi^2$



$\sin^2 2\theta$  vs.  $\Delta\chi^2$



2D contour(NSI pars.)



**Best fit parameters**

$$\varepsilon = 1.0 \times 10^{-3}$$

$$\varepsilon' = -2.7 \times 10^{-2}$$

**Limit from SK-I & SK-II**  
 (90% C.L.)

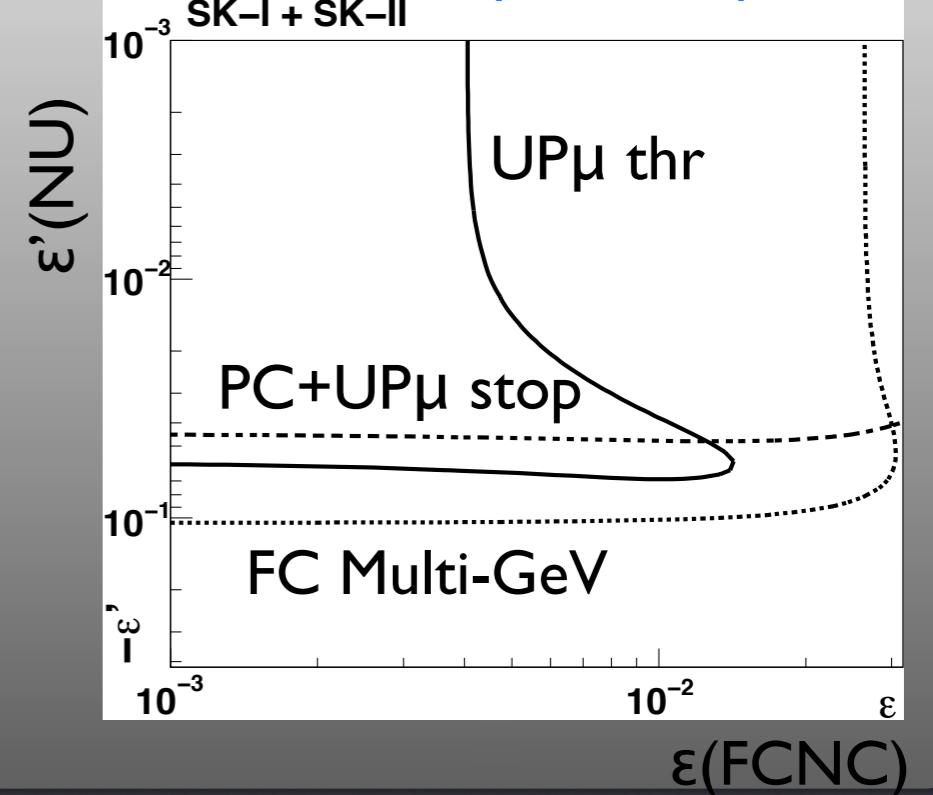
$$|\varepsilon| < 1.1 \times 10^{-2}$$

$$|\varepsilon'| < 4.9 \times 10^{-2}$$

$$\varepsilon = \text{FCNC}$$

$$\varepsilon' = \text{NU}$$

2D contour by sub-samples





# 3-Flavor Hybrid(e $\tau$ sector)

## 3-Flavor Hybrid model

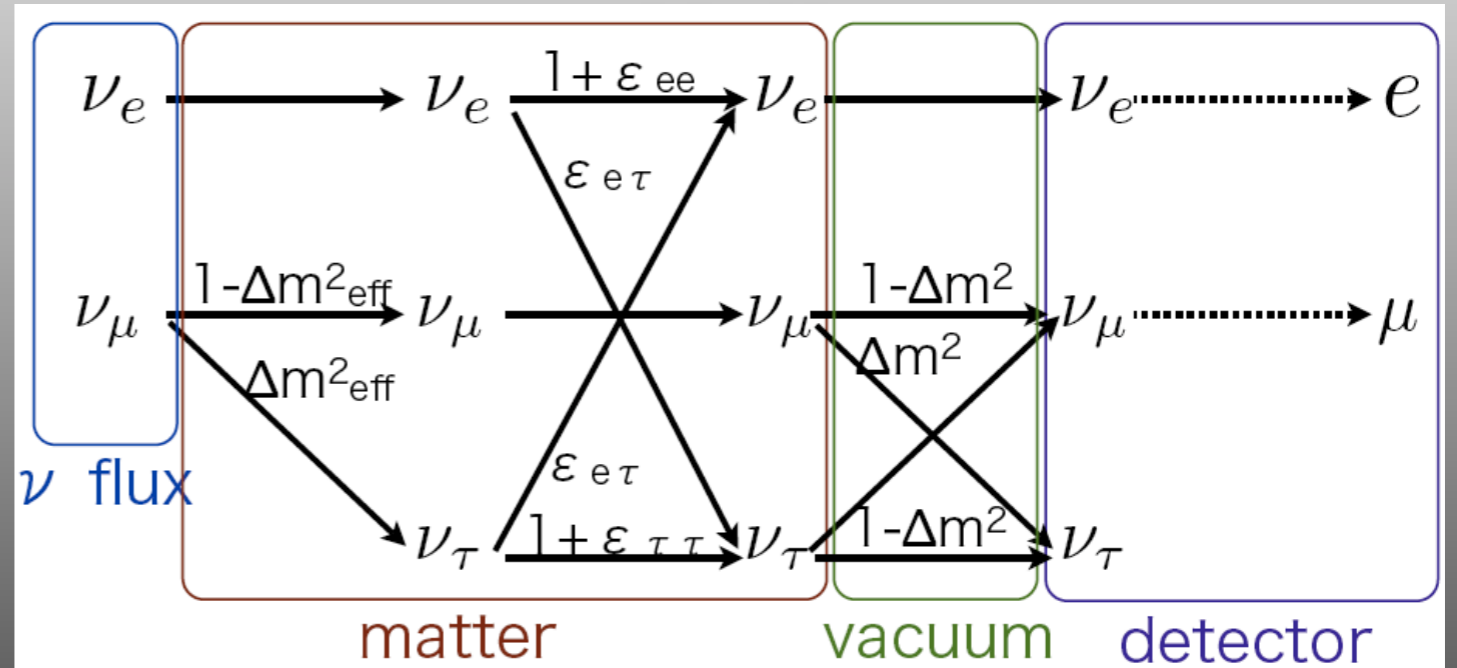
= 2-flavor OSC.(2 $\leftrightarrow$ 3) + 2-flavor NSI(e $\tau$ )

### NSI Hamiltonian

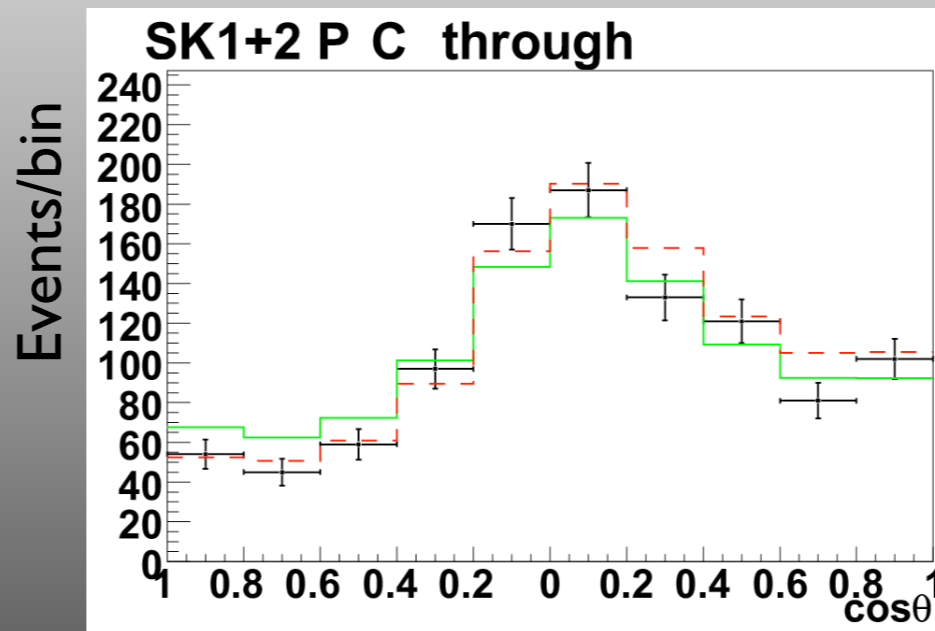
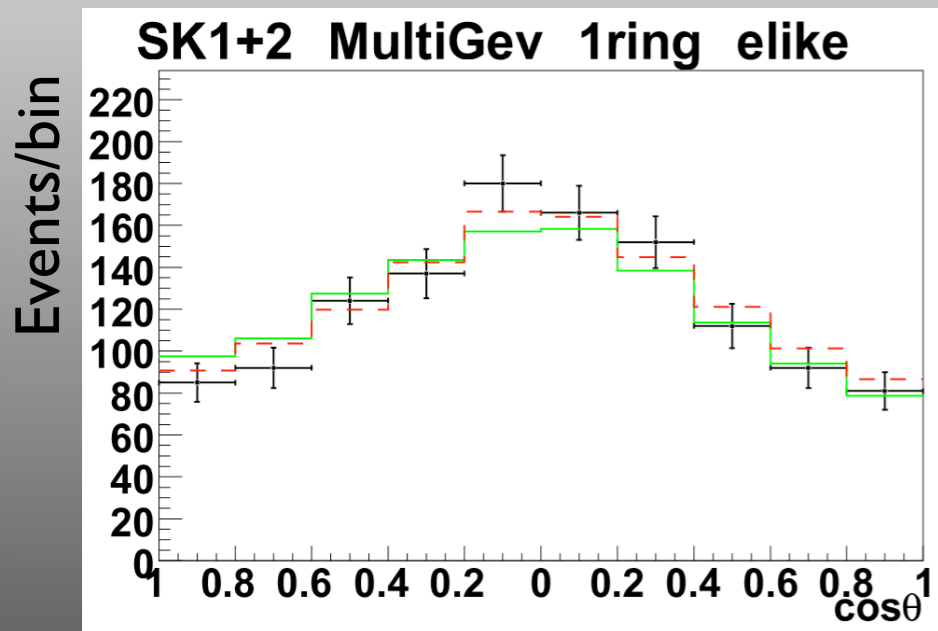
$$H_{\alpha\beta}^{NSI} = \sqrt{2}G_F N_f(\vec{r}) \begin{pmatrix} \boxed{\epsilon_{ee}} & \epsilon_{e\mu}^* & \boxed{\epsilon_{e\tau}^*} \\ \epsilon_{e\mu} & \epsilon_{\mu\mu} & \epsilon_{\mu\tau}^* \\ \boxed{\epsilon_{e\tau}} & \epsilon_{\mu\tau} & \boxed{\epsilon_{\tau\tau}} \end{pmatrix}$$

Focusing only on e $\tau$  sector

Flavor transition from source to detector



Zenith angle distributions with typical parameters



Red : Standard oscillation

Green : NSI

$$\epsilon_{ee} = 0.0$$

$$\epsilon_{e\tau} = 0.2$$

$$\epsilon_{\tau\tau} = 0.2$$

Note : All lines after  $\chi^2$  fitting with systematics.

# 3-Flavor Hybrid(e $\tau$ sector)

Note : No constraint to  $\epsilon_{ee}$  can be given by atm- $\nu$ . External constraint by CHARM is added( $-0.6 < \epsilon_{ee} < 0.5$ ).

Best fit parameters

$$\Delta m^2 = 2.1 \times 10^{-3} \text{eV}^2$$

$$\sin^2 2\theta = 1.0$$

$$\epsilon_{ee} = -0.25$$

$$\epsilon_{e\tau} = 0.016$$

$$\epsilon_{\tau\tau} = 0.024$$

Limit from SK-I & SK-II

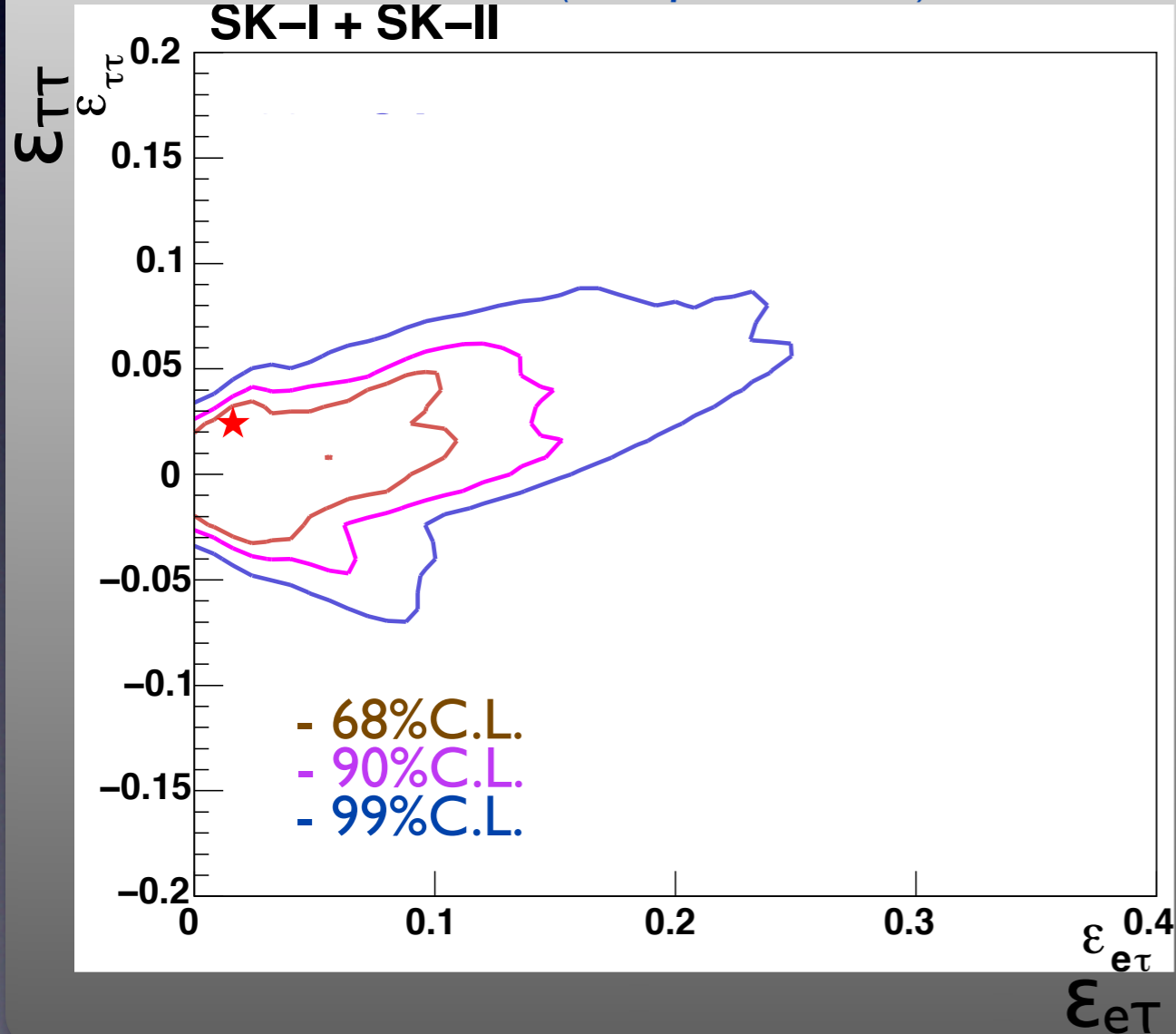
(90% C.L.)

$$|\epsilon_{e\tau}| < 0.16$$

$$-0.05 < \epsilon_{\tau\tau} < 0.06$$

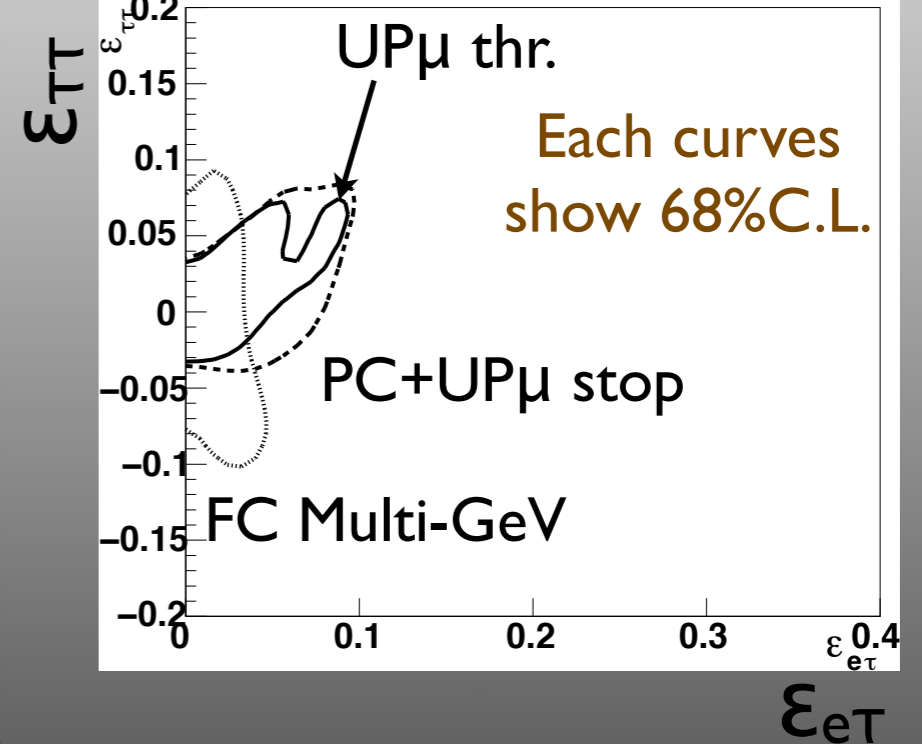
2D contour(NSI parameters)

SK-I + SK-II



2D contour by sub-samples

SK-I + SK-II





# Constraints by SK

Note :Atm-ν cannot distinguish “L” and “R”.

$$\varepsilon_{\alpha\beta} = \varepsilon_{\alpha\beta}^{dL} + \varepsilon_{\alpha\beta}^{dR}$$

Existing limits

CHARM(90%C.L.)

$$|\varepsilon_{e\tau}^{dL}| < 0.5$$

$$|\varepsilon_{e\tau}^{dR}| < 0.5$$

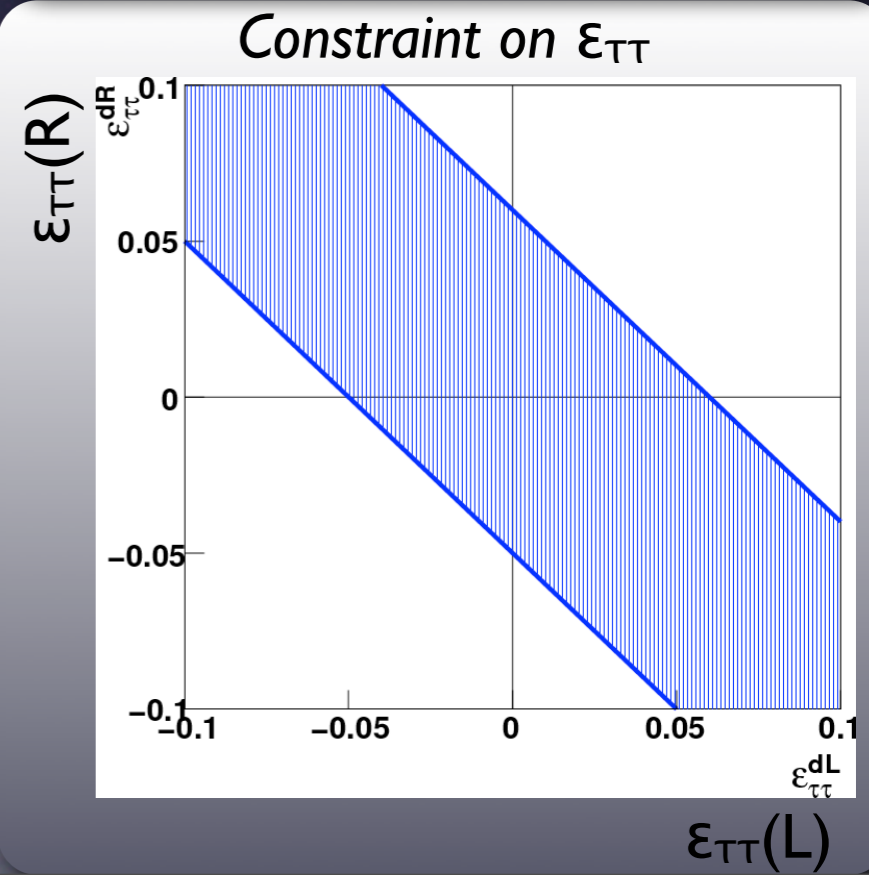
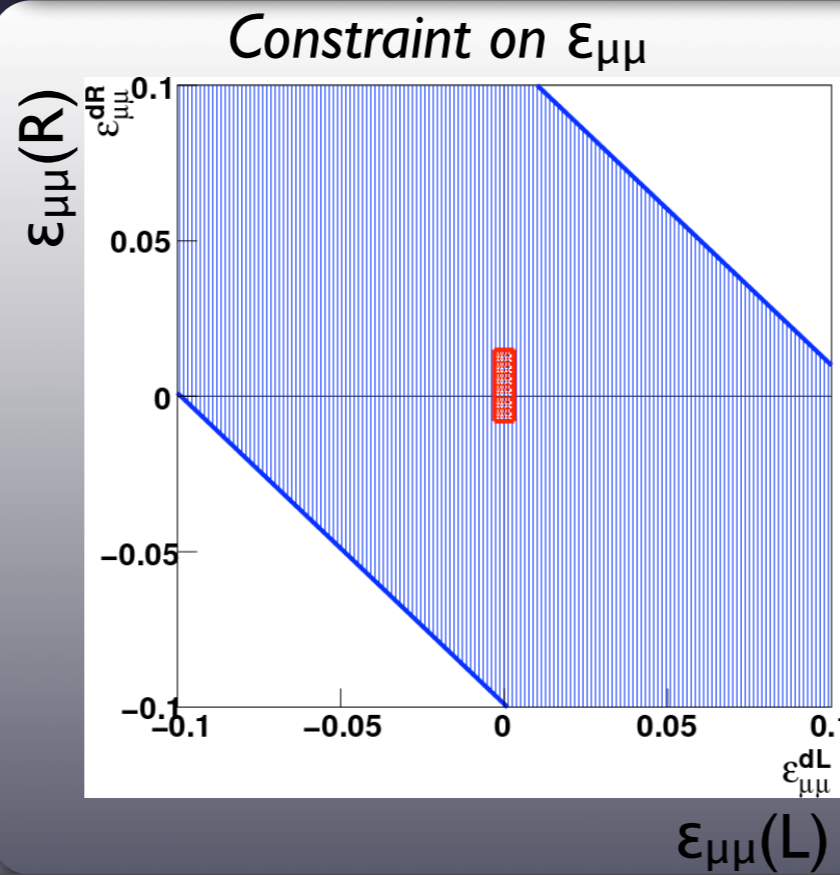
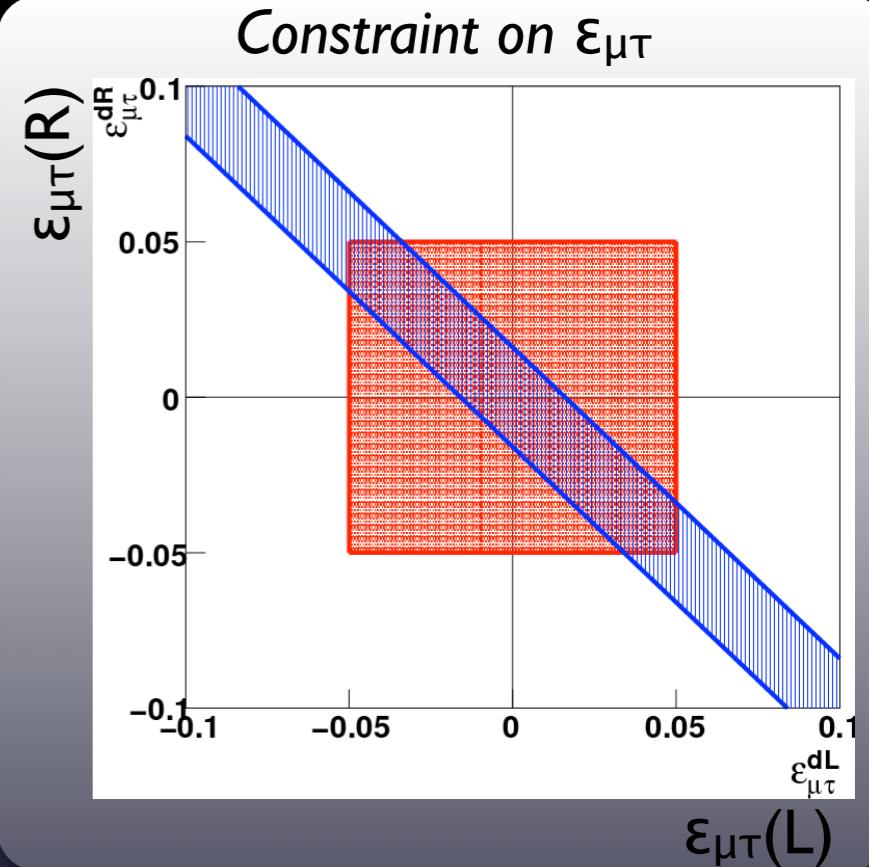
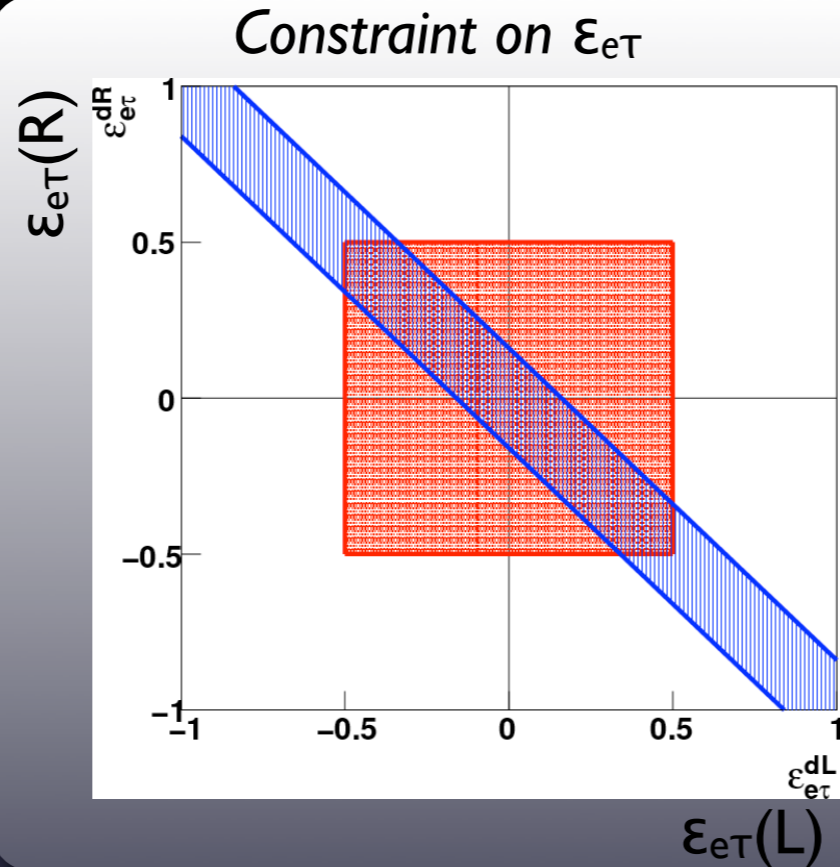
NuTeV(90%C.L.)

$$|\varepsilon_{\mu\mu}^{dL}| < 0.003$$

$$-0.008 < \varepsilon_{\mu\mu}^{dR} < 0.015$$

$$|\varepsilon_{\mu\tau}^{dL}| < 0.05$$

$$|\varepsilon_{\mu\tau}^{dR}| < 0.05$$



# Conclusion

- $\nu$  oscillation is stable even with additional NSI term.
- NSI is consistent with 0.
- Limit on FCNC is tighter by an order of magnitude.
- Limit on  $\text{NU}(\tau\tau)$  is significantly improved.



Backup



# What is NSI ?

- NSI : Interaction between a given particle and another one beyond standard model
- NSI is studied in neutrino as well as top-pair and decay etc...



# Theorists' opinions

- Hybrid mode with oscillation and NSI can be expected, where NSI is contained as sub-dominant channel[1,2]
- Large value is theoretically allowed in  $e\tau$  channel[3]
- Loose limit on  $e\tau$  channel can spoils the sensitivity of  $\theta_{13}$ [3,4]  
[1] N. Fornengo et al., Phys. Rev. D65 (2002) 013010 [hep-ph/0108043]  
[2] M. C. Gonzalez-Garcia and M. Maltoni,



## Hybrid model with oscillation and NSI

We follow the formalism by M. C. Gonzalez-Garcia  
and Michele Maltoni in PRD 70, 033010 (2004)

$$H = \underbrace{\frac{\Delta m_{23}^2}{4E} R_\theta \begin{pmatrix} -1 & 0 \\ 0 & 1 \end{pmatrix}}_{\text{oscillation}} \pm \underbrace{\sqrt{2} G_F N_r(r) R_\phi \begin{pmatrix} -1 & 0 \\ 0 & 1 \end{pmatrix} R_\phi}_{\text{NSI}}$$

where  $R_\theta = \begin{pmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{pmatrix}$   $R_\phi = \begin{pmatrix} \cos \phi & \sin \phi \\ -\sin \phi & \cos \phi \end{pmatrix}$   $\phi = \frac{1}{2} \arctan \left( \frac{\varepsilon}{\varepsilon'/2} \right)$

Survival probability

$$P_{\nu_\mu \rightarrow \nu_\mu} = 1 - \sin^2 2\Theta \sin^2 \left( \frac{\Delta m^2 L}{4E} R \right)$$

where

$$\sin^2 2\Theta = \frac{1}{R^2} \left( \sin^2 2\theta + R^2 \sin^2 2\phi + 2R \sin 2\theta \sin 2\phi \cos \eta \right)$$

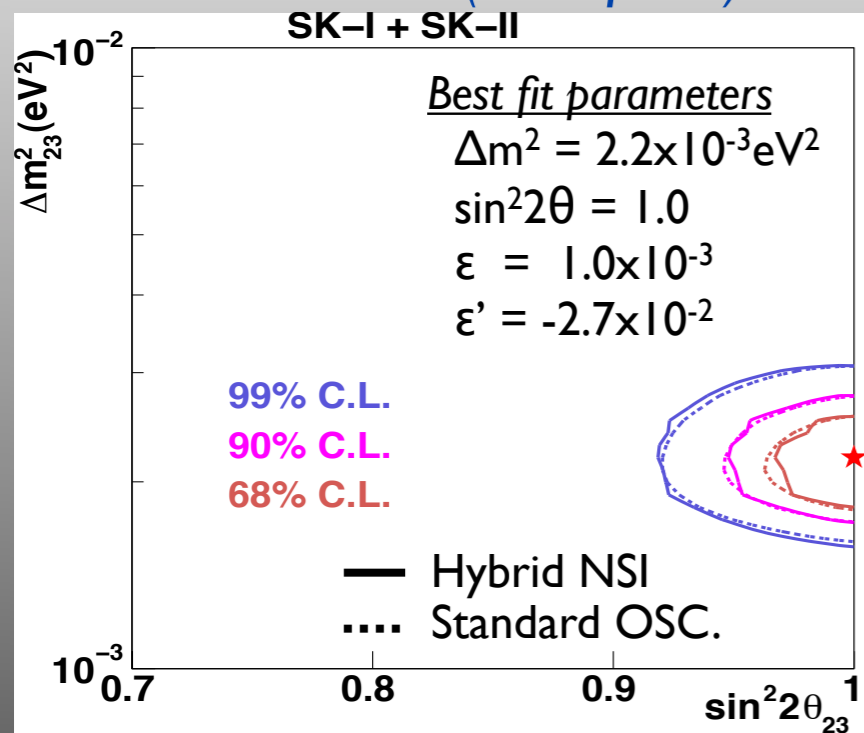
$$R = \sqrt{1 + R^2 + 2R(\cos 2\theta \cos 2\phi + \sin 2\theta \sin 2\phi \cos \eta)}$$

Scanning parameters  
 $\sin 2\theta, \Delta m^2$  (for osc.)  
 relative phase:  
 $\varepsilon, \varepsilon', \cos \eta$  (for NSI)  
 $\eta = \arg(\varepsilon)$

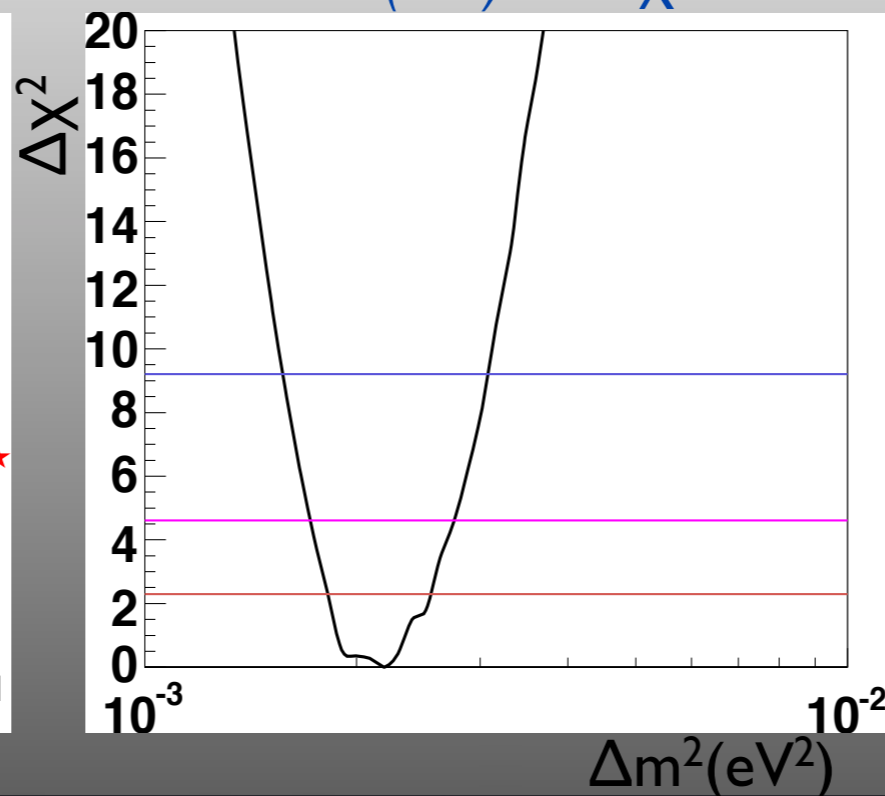


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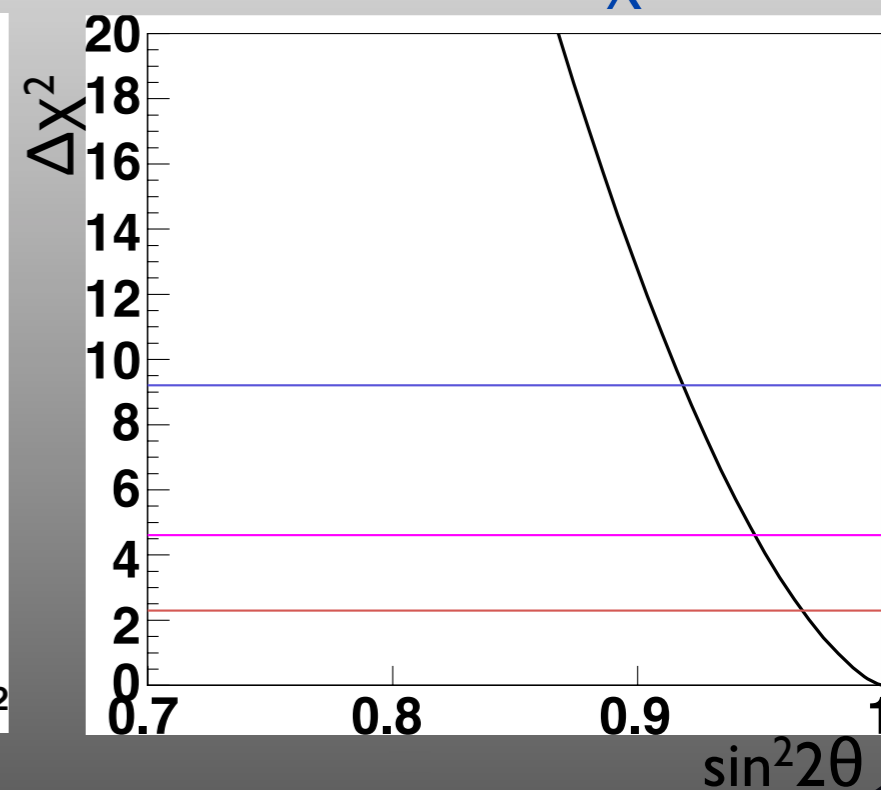
2D contour(OSC pars.)



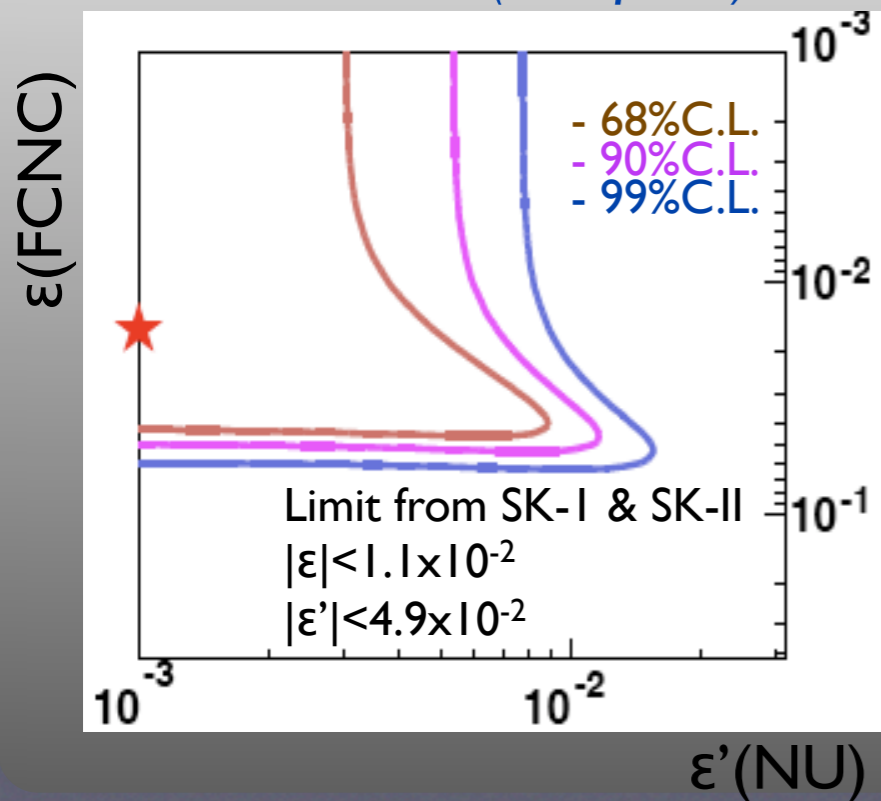
$\Delta m^2(\text{eV}^2)$  vs.  $\Delta\chi^2$



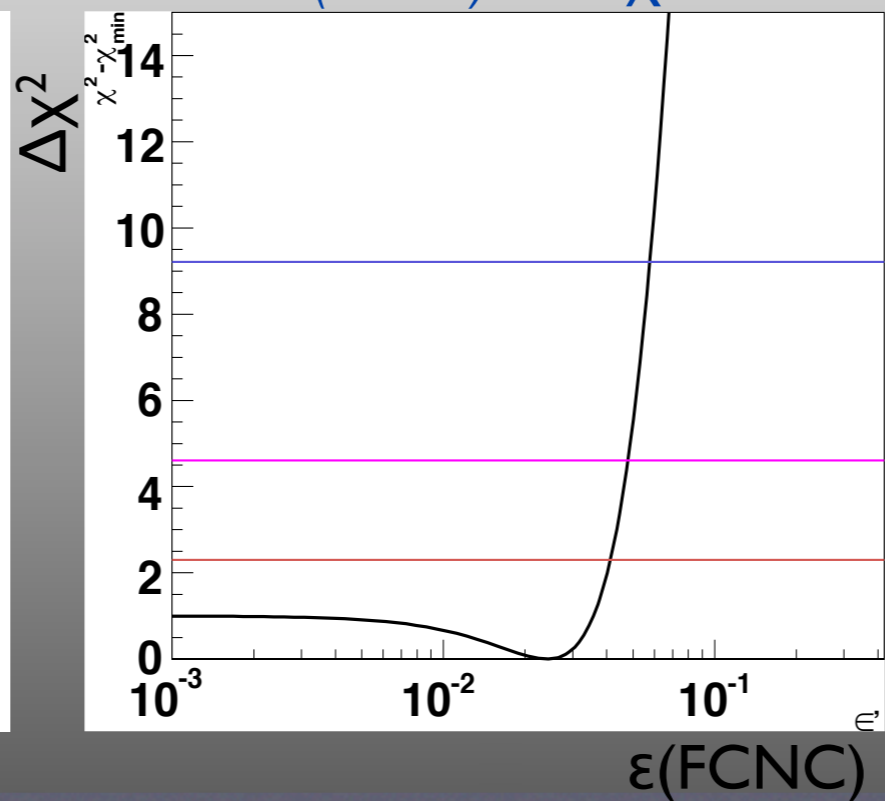
$\sin^2 2\theta$  vs.  $\Delta\chi^2$



2D contour(NSI pars.)



$\epsilon(\text{FCNC})$  vs.  $\Delta\chi^2$



$\epsilon'(\text{NU})$  vs.  $\Delta\chi^2$

